



# The proton form factors at low $Q^2$

**new results and future measurements**

Guy Ron  
Hebrew University of Jerusalem

*Short Range Correlations in Nuclei and Hard QCD Phenomena, Trento  
Nov 16, 2011*



# The proton form factors at low $Q^2$

## new results and future measurements

Coffee break 10:45 – 11:15

11:15 Daniele Treleani

*"Collisions of protons with light nuclei shed new light on nucleon structure"*

11:40 Guy Ron

*"The proton form factors at low  $Q^2$  - new results and future measurements"*

Sho

LUNCH BREAK 12:45 – 2:00



**INTERNATIONAL WORKSHOP**  
**on**  
**SHORT RANGE CORRELATIONS IN NUCLEI AND HARD QCD**  
**PHENOMENA**

**ECT\*, Trento, November 14-18, 2011**

**DRAFT of the PROGRAM**

(talks 25' + 10' discussion)

Coffee break 10:45 – 11:15

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*"Collisions of protons with light nuclei shed new light on nucleon structure"*

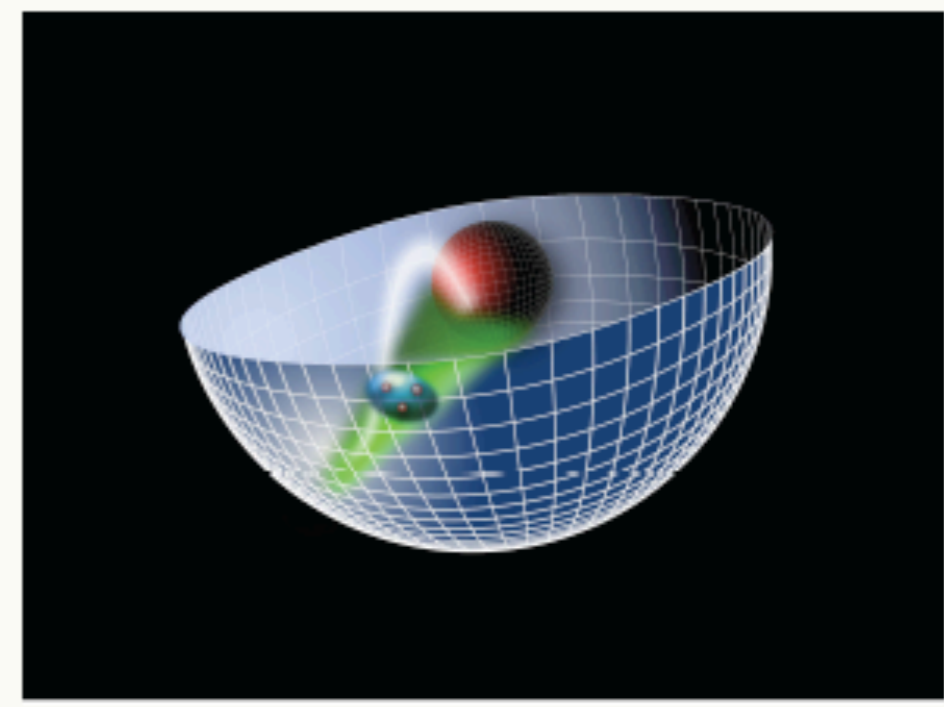
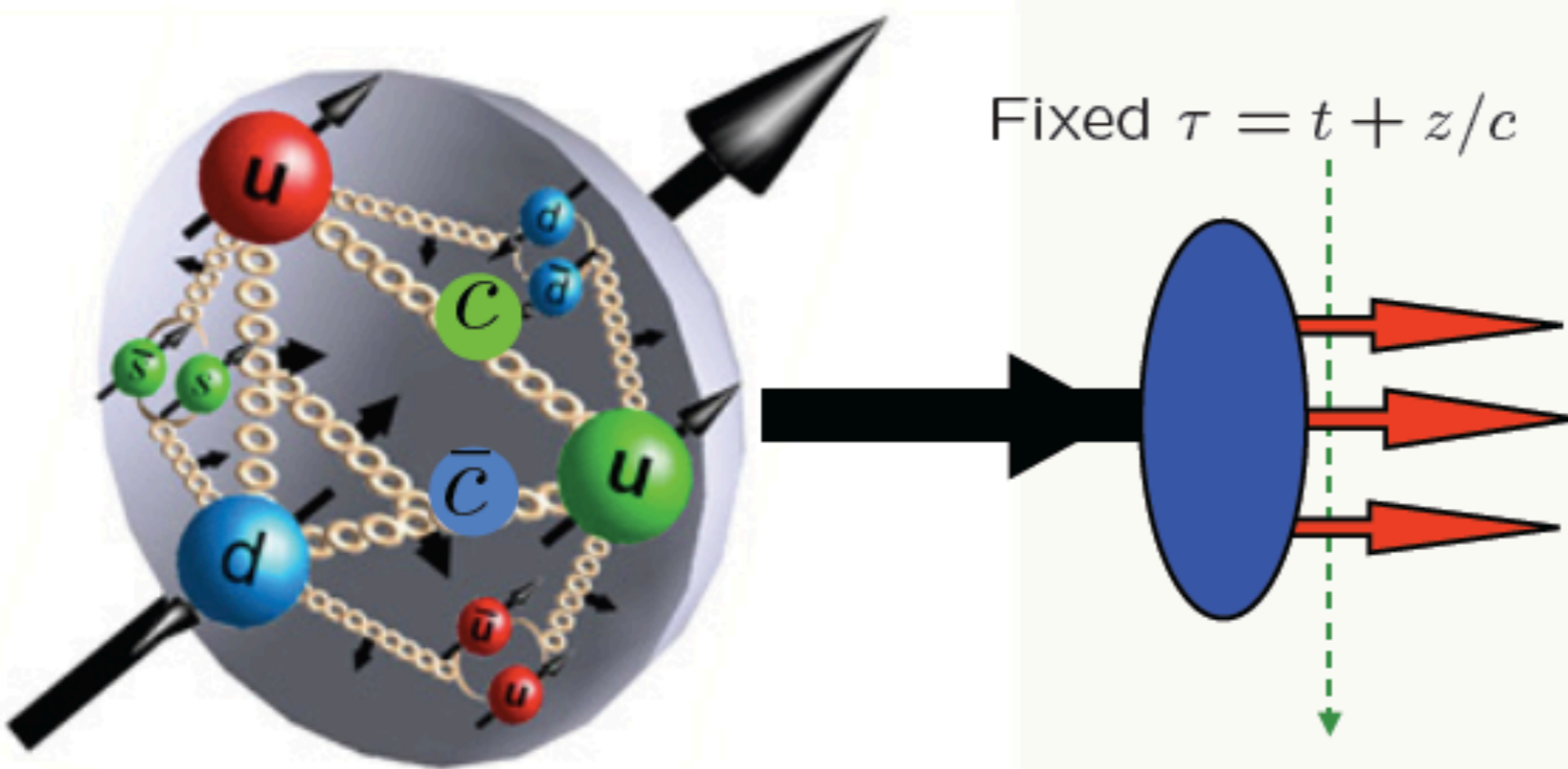
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*"The proton form factors at low  $Q^2$  - new results and future measurements"*

LUNCH BREAK 12:45 – 2:00

Sho

# Light-Front Holography and Novel QCD Phenomena



## Light-Cone 2011 Applications of light-cone coordinates to highly relativistic systems



Stan Brodsky





# The proton form factors at low $Q^2$

**new results and future measurements**

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Nov 16, 2011*

# OUTLINE

- Nucleon Structure 101.
- Measuring the nucleon Form Factors.
- Experimental Results.
- Impacts.

# NUCLEON STRUCTURE

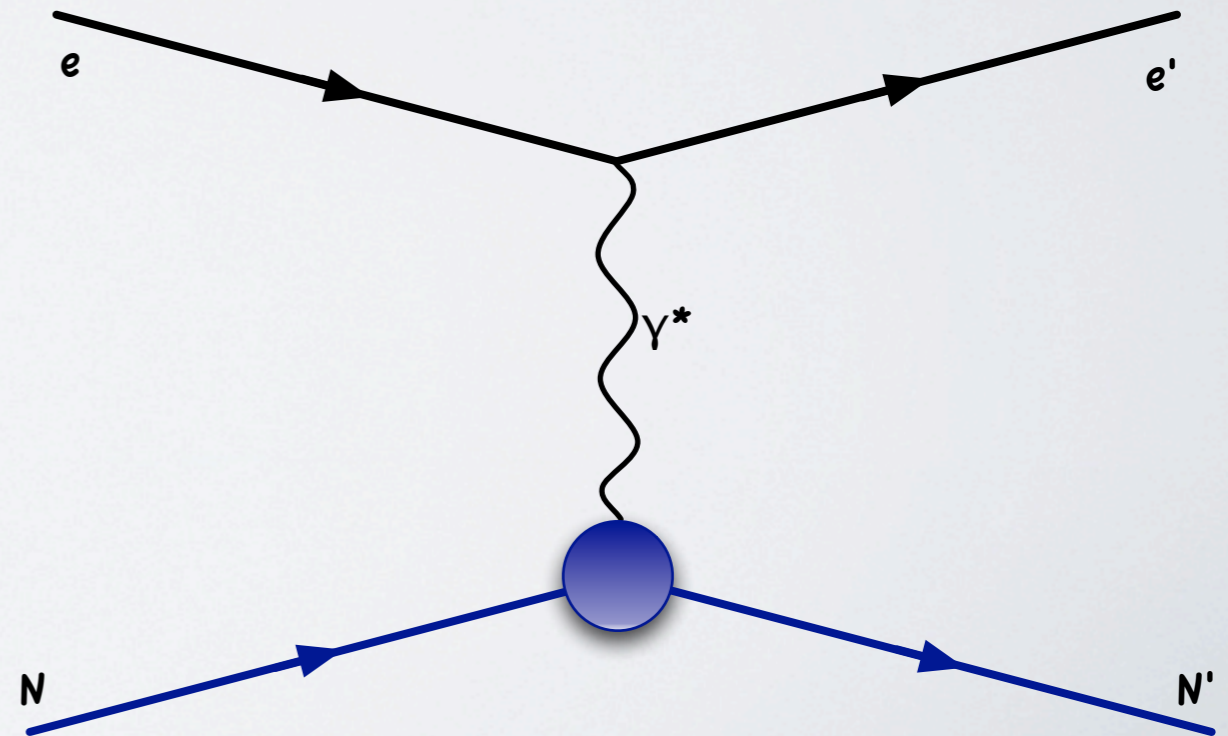
- Nucleons are spin-1/2 particles.
- But measured magnetic moment is  $\mu_p \sim 2.793\mu_N$   
 $\mu_n \sim -1.91\mu_N$
- Nucleons are **not pointlike** (also known from Deep Inelastic Scattering).
- Complex internal structure generated by interactions between pointlike (dressed?) constituents (quarks / partons).
- Even more complex behavior comes from virtual constituents (“sea” quarks, gluons).

# ELECTRON SCATTERING CROSS-SECTION (1- $\gamma$ )

$$\frac{d\sigma_R}{d\Omega} = \frac{\alpha^2}{Q^2} \left( \frac{E'}{E} \right)^2 \frac{\cot^2 \frac{\theta_e}{2}}{1 + \tau}$$

Rutherford - Point-Like

$$\tau = \frac{Q^2}{4M^2}, \quad \varepsilon = \left[ 1 + 2(1 + \tau) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$





# ELECTRON SCATTERING CROSS-SECTION (1- $\gamma$ )

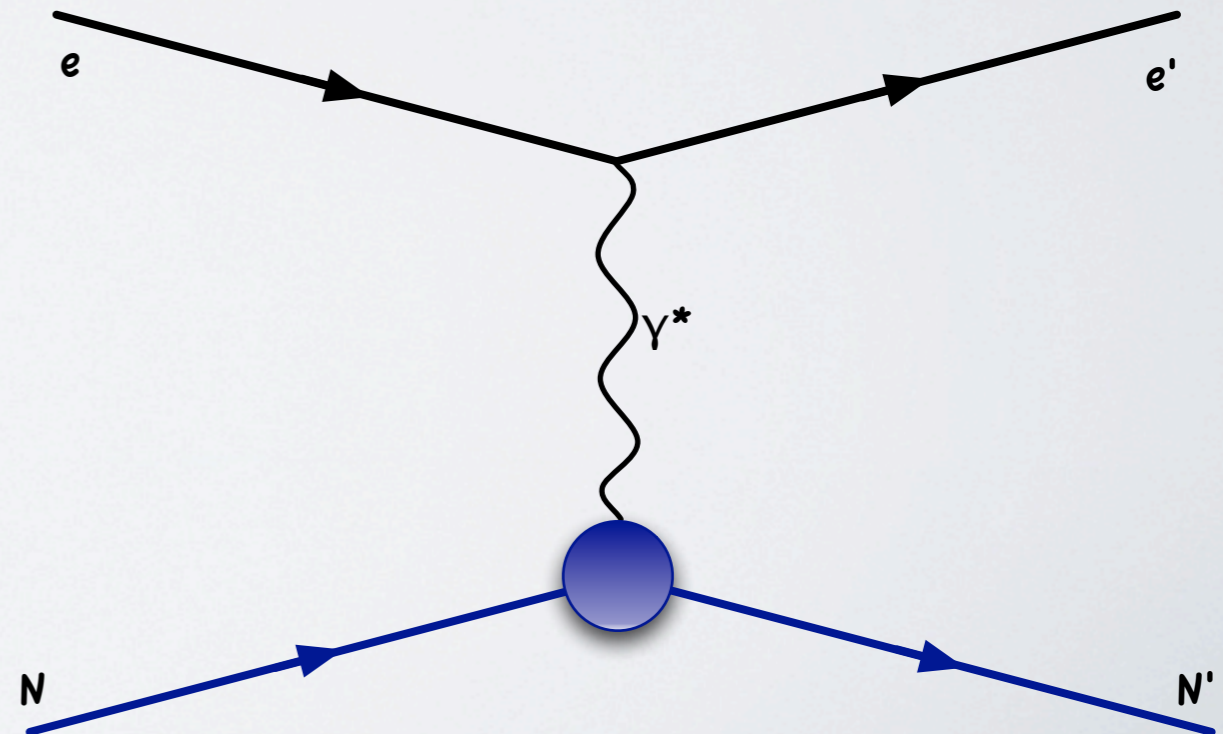
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Rutherford - Point-Like

$$\frac{d\sigma_M}{d\Omega} = \frac{d\sigma_R}{d\Omega} \times \left[ 1 + 2\tau \tan^2 \frac{\theta}{2} \right]$$

Mott - Spin-1/2

$$\tau = \frac{Q^2}{4M^2}, \quad \varepsilon = \left[ 1 + 2(1 + \tau) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$



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$$\frac{d\sigma_{Str}}{d\Omega} = \frac{d\sigma_M}{d\Omega} \times \left[ G_E^2(Q^2) + \frac{\tau}{\varepsilon} G_M^2(Q^2) \right]$$

Rosenbluth -  
Spin-1/2 with  
Structure

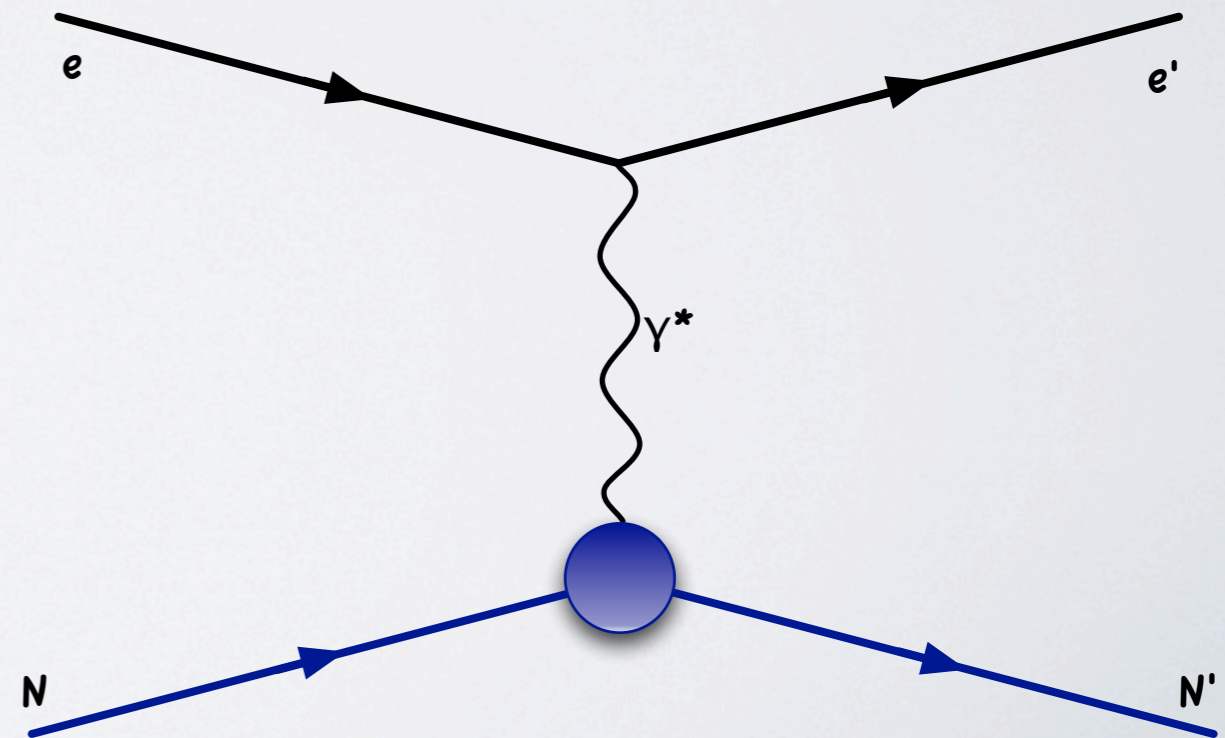
$$\tau = \frac{Q^2}{4M^2}, \quad \varepsilon = \left[ 1 + 2(1 + \tau) \tan^2 \frac{\theta_e}{2} \right]^{-1}$$

$$G_E^p(0) = 1 \quad G_E^n(0) = 0$$

$$G_M^p = 2.793 \quad G_M^n = -1.91$$

Sometimes  
written using:

$$G_E = F_1 - \tau F_2$$

$$G_M = F_1 + F_2$$


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Everything we don't know goes here!

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Spin-1/2 with  
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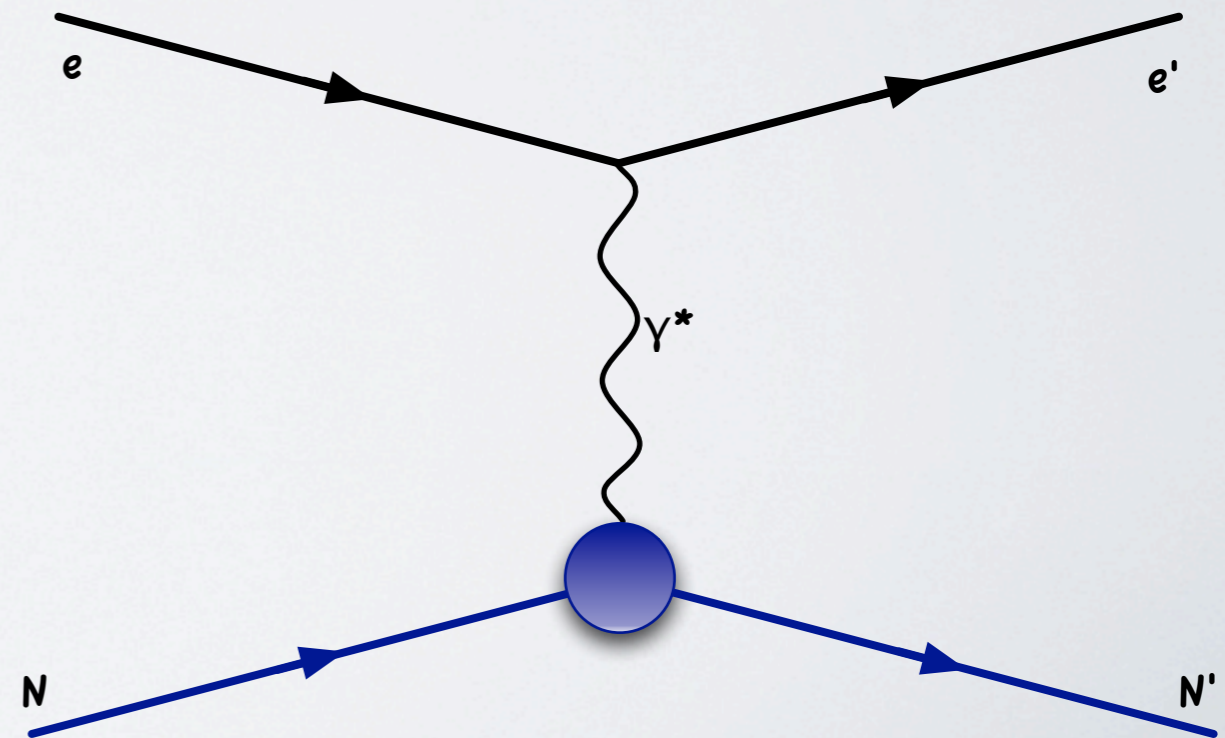
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## IN THE BREIT FRAME...

*It can be shown that...*

*The Hadronic Current*

$$\mathcal{J}^0 = ie\bar{v}(p') \left[ (F_1 + \kappa F_2) \gamma^0 - \frac{E_{pB}}{m} \kappa F_2 \right] v(p)$$

$$\vec{\mathcal{J}} = ie (F_1 + \kappa F_2) \bar{v}(p') \vec{\gamma} v(p)$$

*Explicitly*

$$\mathcal{J}^0 = ie2m\chi'^{\dagger} \chi (F_1 - \tau\kappa F_2) = ie2m\chi'^{\dagger} \chi G_E$$

$$\vec{\mathcal{J}} = -e\chi'^{\dagger} (\vec{\sigma} \times \vec{q}_B) \chi (F_1 + \kappa F_2) = -e\chi'^{\dagger} (\vec{\sigma} \times \vec{q}_B) \chi G_M$$

*Sachs Form Factors related to electric and magnetic part of the interaction - in the Breit Frame.*

# THE NAIVE INTERPRETATION

$$\begin{aligned}G_E(Q^2) &= \int \rho_{Ch}(\vec{r}) e^{i\vec{q}\cdot\vec{r}} d^3r \\ &\sim \int \rho_{Ch}(\vec{r}) d^3r - \frac{q^2}{6} \int \rho_{Ch}(\vec{r}) r^2 d^3r + \dots \\ &\sim Ch - \frac{q^2}{6} \langle r^2 \rangle_{Ch} + \dots \\ G_M(Q^2) &= \int \rho(\vec{r})_M e^{i\vec{q}\cdot\vec{r}} d^3r \\ &\sim \mu - \frac{q^2}{6} \langle r^2 \rangle_M + \dots\end{aligned}$$

As wrong as you can be while still being somewhat right...

# What we know

- Experimentally found to approximately follow (to about 10%) the dipole form:

$$F_D(Q^2) = (1 + Q^2/0.71)^{-2}$$

- Dipole form in Q space  $\rightarrow$  exponential in r space.
- We know the limiting values at  $Q^2=0$ .
- But... We know that there are deviations from dipole (very pronounced at high  $Q^2$ ).

# Why We Care

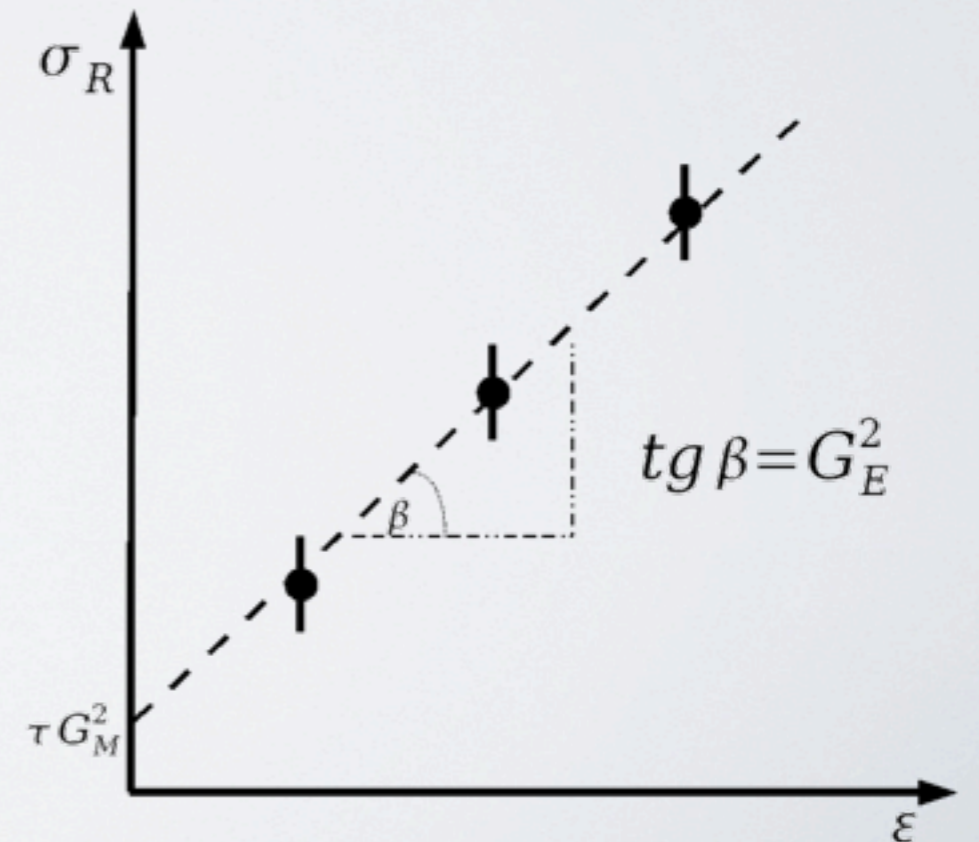
- FF are a basic property of the nucleon, related to the complex internal structure.
- Completely describe the EM structure of the nucleon ground state.
- Comparing  $G_E$  and  $G_M \rightarrow$  difference between spatial distributions of charge and magnetization.
- Input to other calculations (more later).
- Different theories constrained by different  $Q^2$  regions.
- An important place to look for quark/gluon  $\rightarrow$  hadron/meson picture transition.
- EM structure expected to change in the nuclear medium.

# Measurement Techniques

## Rosenbluth Separation

$$\sigma_R = (d\sigma/d\Omega)/(d\sigma/d\Omega)_{\text{Mott}} = \tau G_M^2 + \varepsilon G_E^2$$

- Measure the reduced cross section at several values of  $\varepsilon$  (angle/beam energy combination) while keeping  $Q^2$  fixed.
- Linear fit to get intercept and slope.
- **But...**  $G_M$  suppressed for low  $Q^2$  (and  $G_E$  for high).
- Also normalization issues/acceptance issues/etc. make it hard to get high precision.





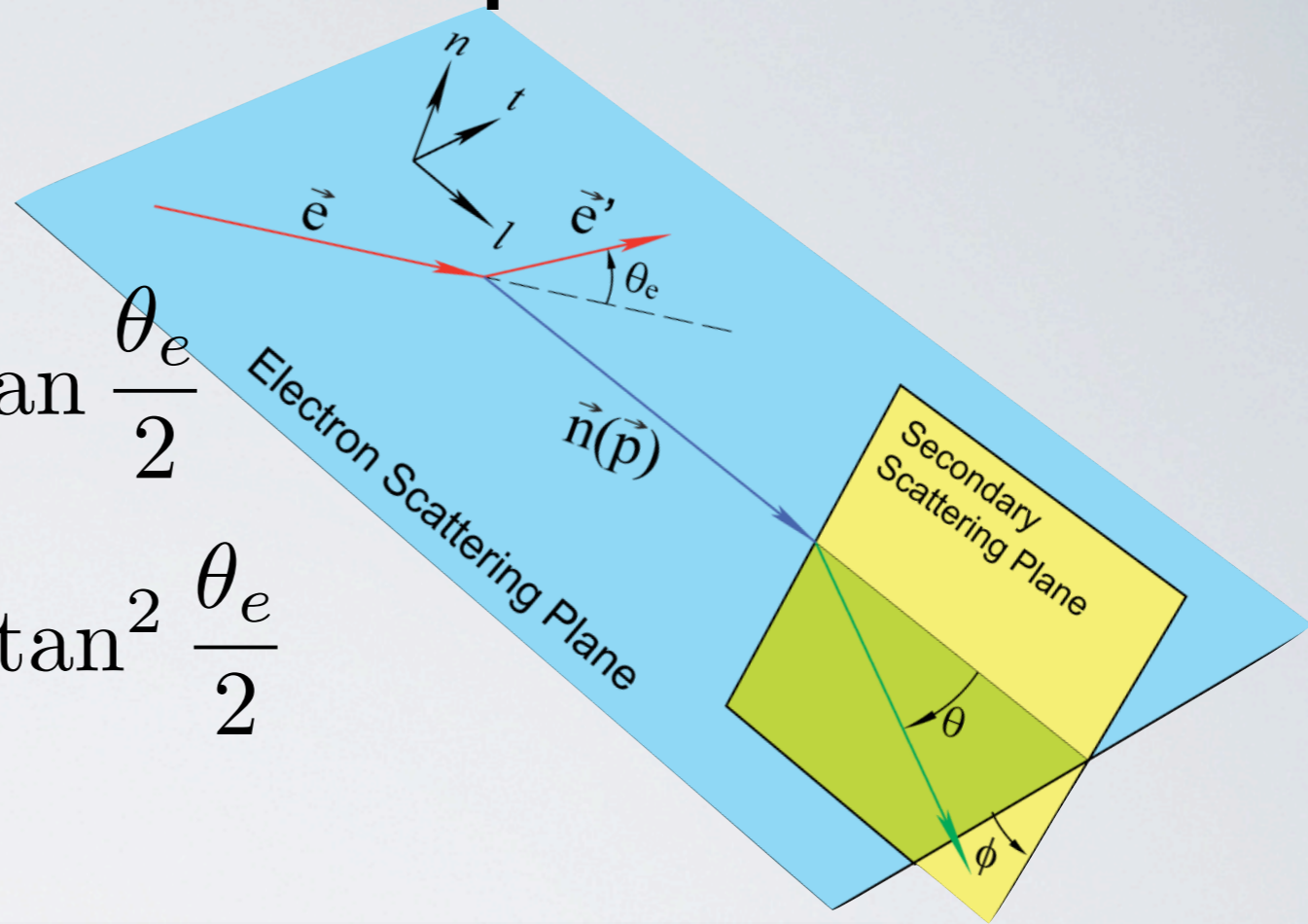
# Measurement Techniques

## Recoil Polarization

$$I_0 P_t = -2\sqrt{\tau(1+\tau)} G_E G_M \tan \frac{\theta_e}{2}$$

$$I_0 P_l = \frac{E_e + E_{e'}}{M} \sqrt{\tau(1+\tau)} G_M^2 \tan^2 \frac{\theta_e}{2}$$

$$P_n = 0 \quad (1\gamma)$$



$$\mathcal{R} \equiv \mu_p \frac{G_E}{G_M} = -\mu_p \frac{P_t}{P_l} \frac{E_e + E_{e'}}{2M} \tan \frac{\theta_e}{2}$$

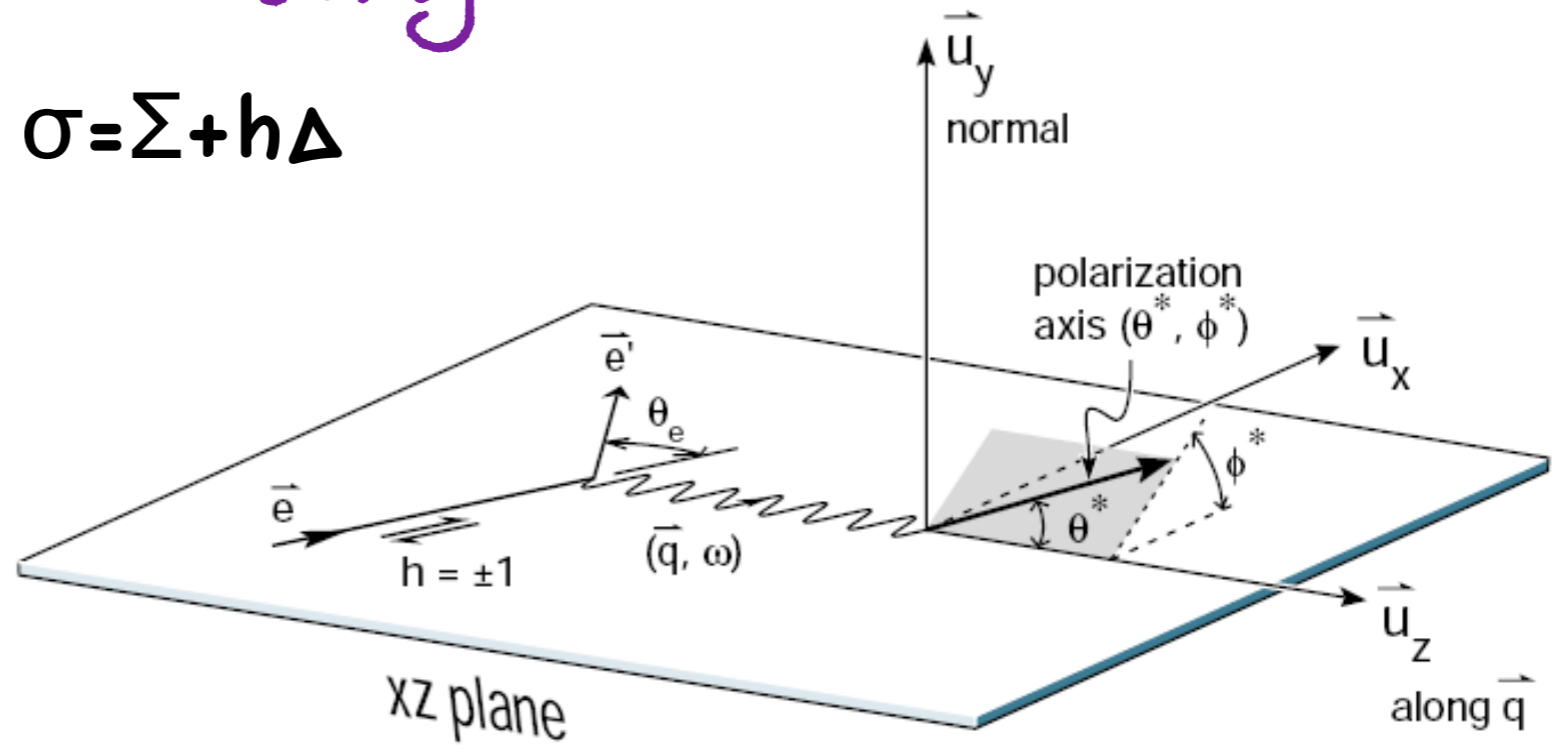
- A single measurement gives ratio of form factors.
- Interference of "small" and "large" terms allow measurement at practically all values of  $Q^2$ .

# Measurement Techniques

## Beam-Target Asymmetry

Polarized Cross Section:  $\sigma = \Sigma + h\Delta$

$$A = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

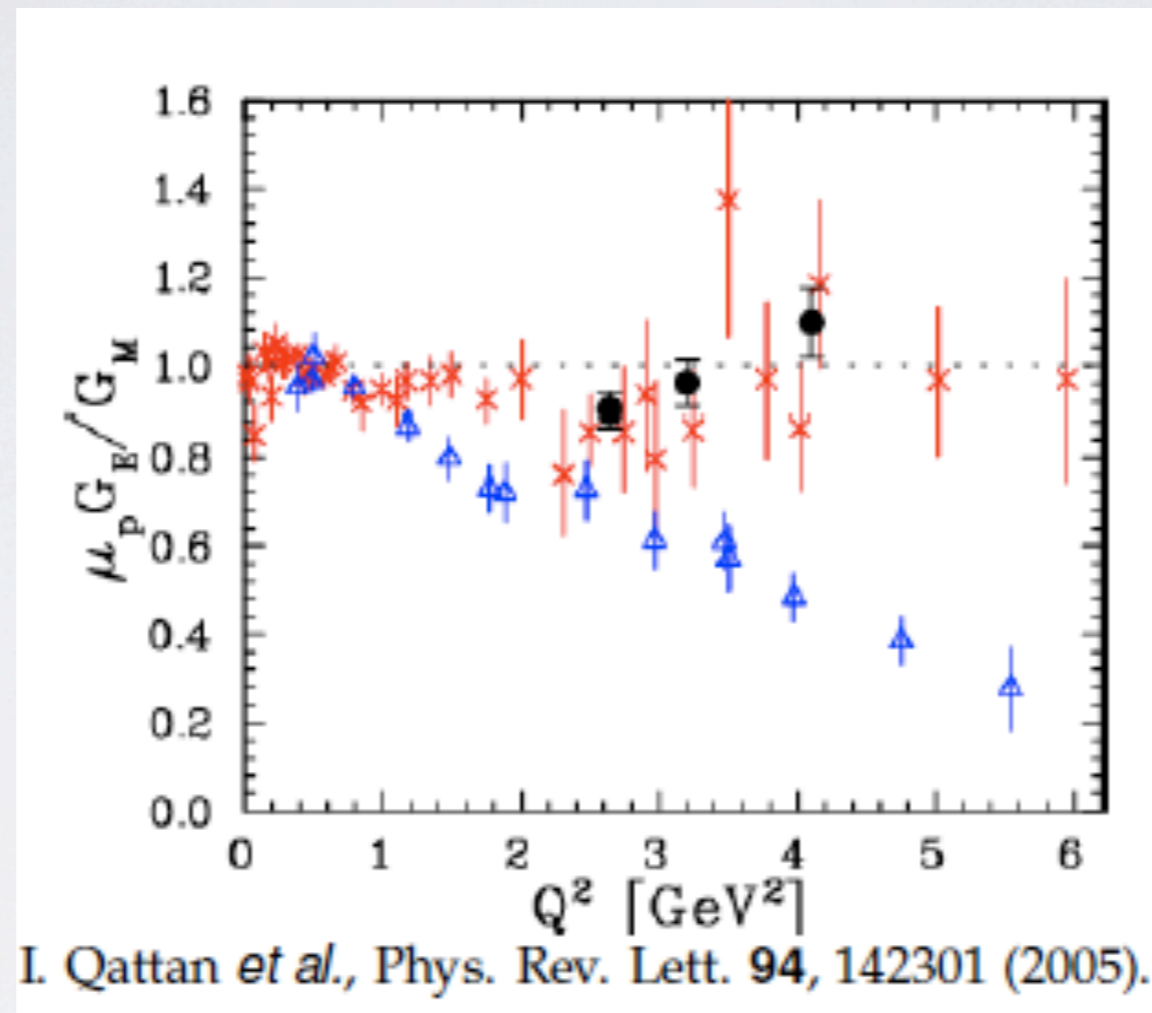


$$A = f P_b P_t \frac{\overbrace{a \cos \theta^* G_M^2}^{A_T} + \overbrace{b \sin \theta^* \cos \phi^* G_E G_M}^{A_{LT}}}{c G_M^2 + d G_E^2}$$

Measure asymmetry at two different target settings, say  $\theta^* = 0, 90$ .  
 Ratio of asymmetries gives ratio of form factors.  
 Functionally identical to recoil polarimetry measurements.

# The high $Q^2$ discrepancy

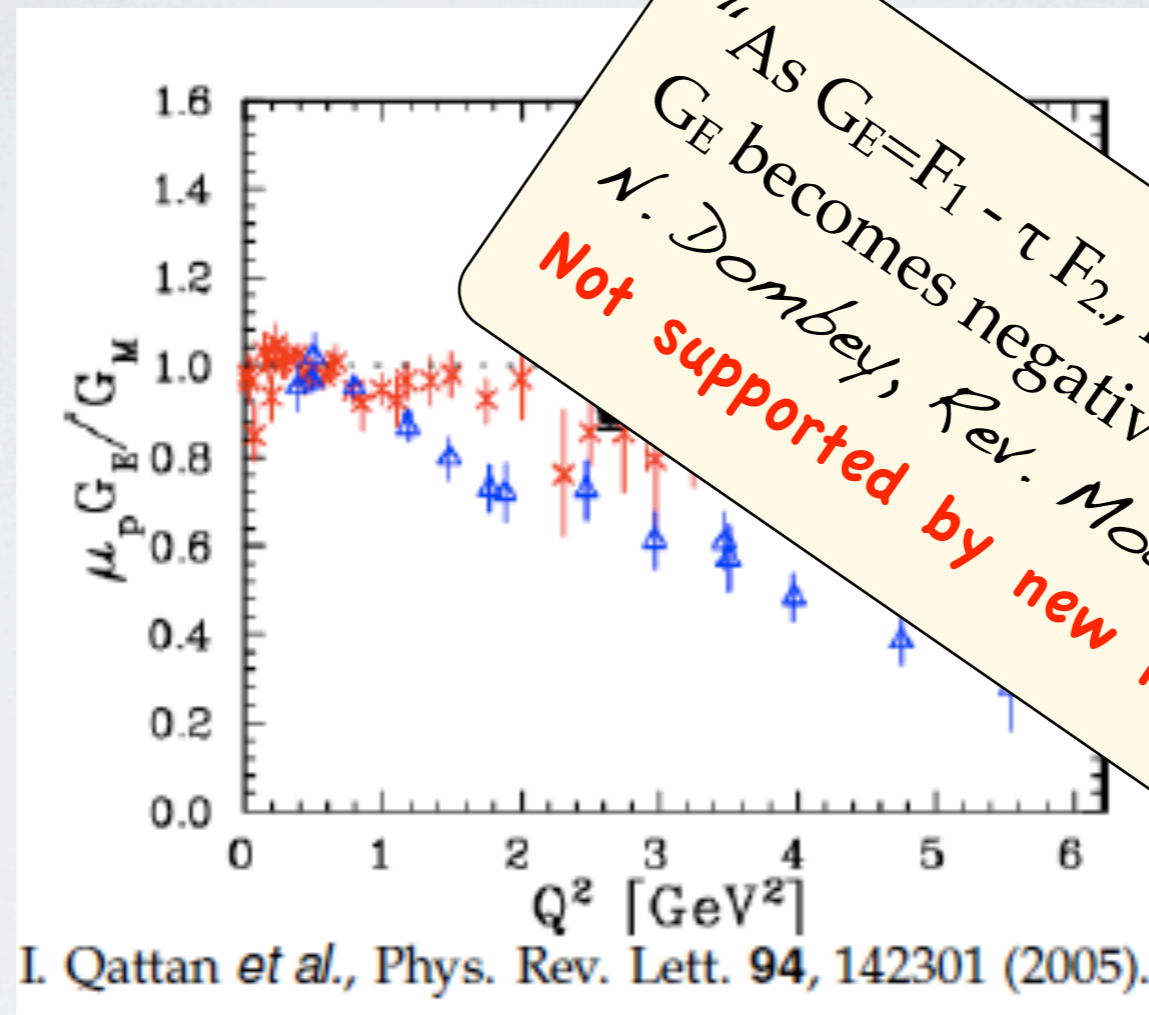
- At high  $Q^2$  Rosenbluth and polarization measurements for the proton are in violent disagreement.



- Almost certainly explained by multi- $\gamma$  effects.
- *But what about low  $Q^2$ ?*

# The high $Q^2$ discrepancy

- At high  $Q^2$  Rosenbluth and polarization measurements for the proton are in violent disagreement.

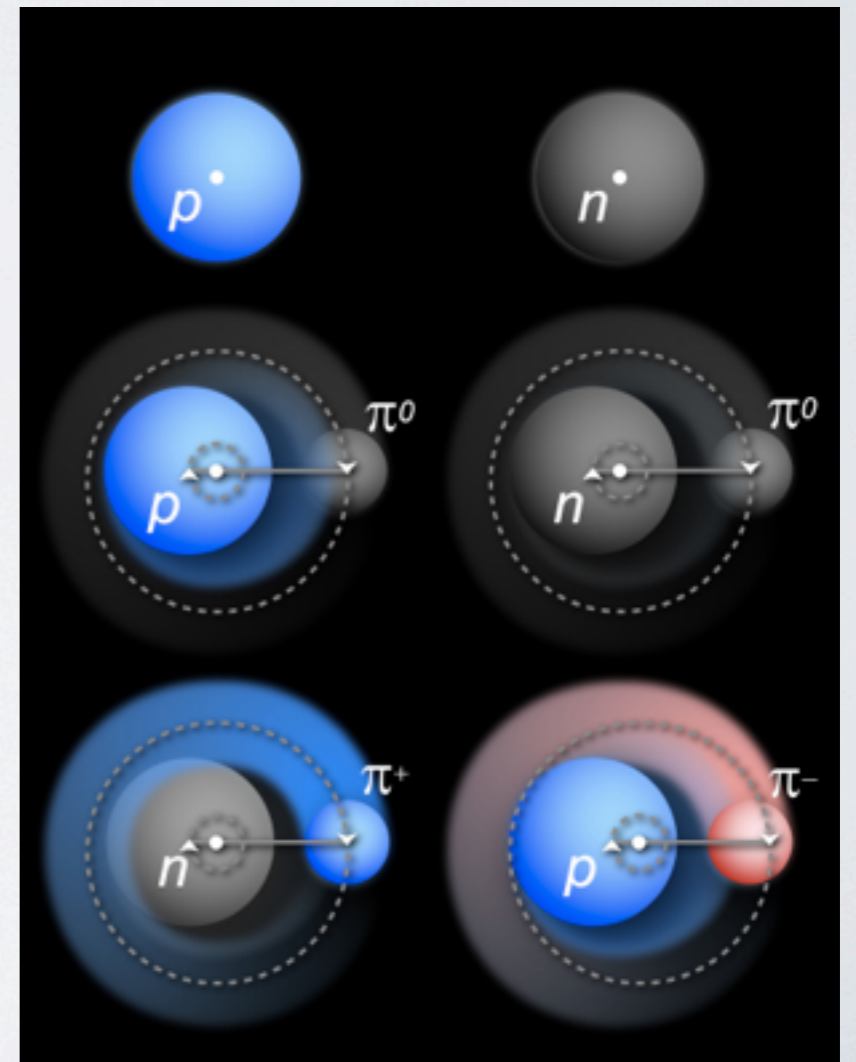


"As  $G_E = F_1 - \tau F_2$ , it is a priori quite likely that  $G_E$  becomes negative for large values of  $k^2$ " -  
N. Dombey, Rev. Mod. Phys. 41, 1 (1969). -  
**Not supported by new results.**

- Almost certainly explained by multi- $\gamma$  effects.
- *But what about low  $Q^2$ ?*

# Why Low $Q^2$ ?

- Deviations from dipole form evident.
- Probe static properties ( $Q^2 \rightarrow 0$ ) and peripheral structure.
- Small  $Q^2$  does not allow for pQCD, many competing EFTs.
- Hitting the  $\pi$  mass region.
- Potentially impacts many high precision measurements (nucleon GPDs, parity violation, Zemach radius,...).

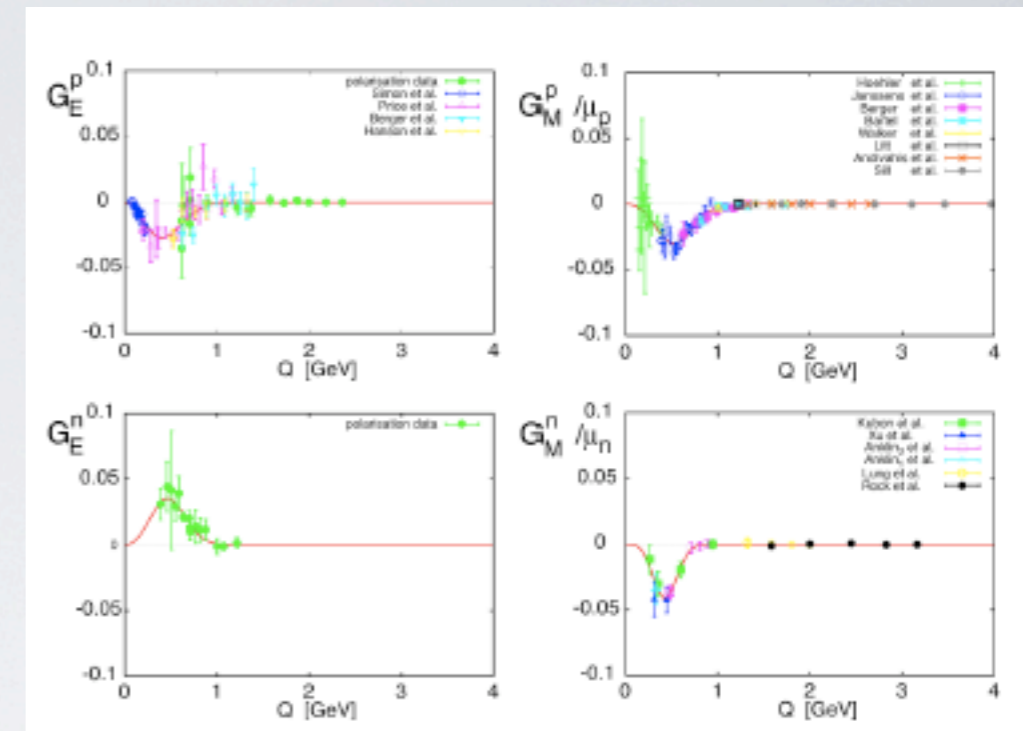


# LOW $Q^2$ Notable Results

## Friedrich & Walcher analysis

*Eur. Phys. J. A17, 607 (2003)*

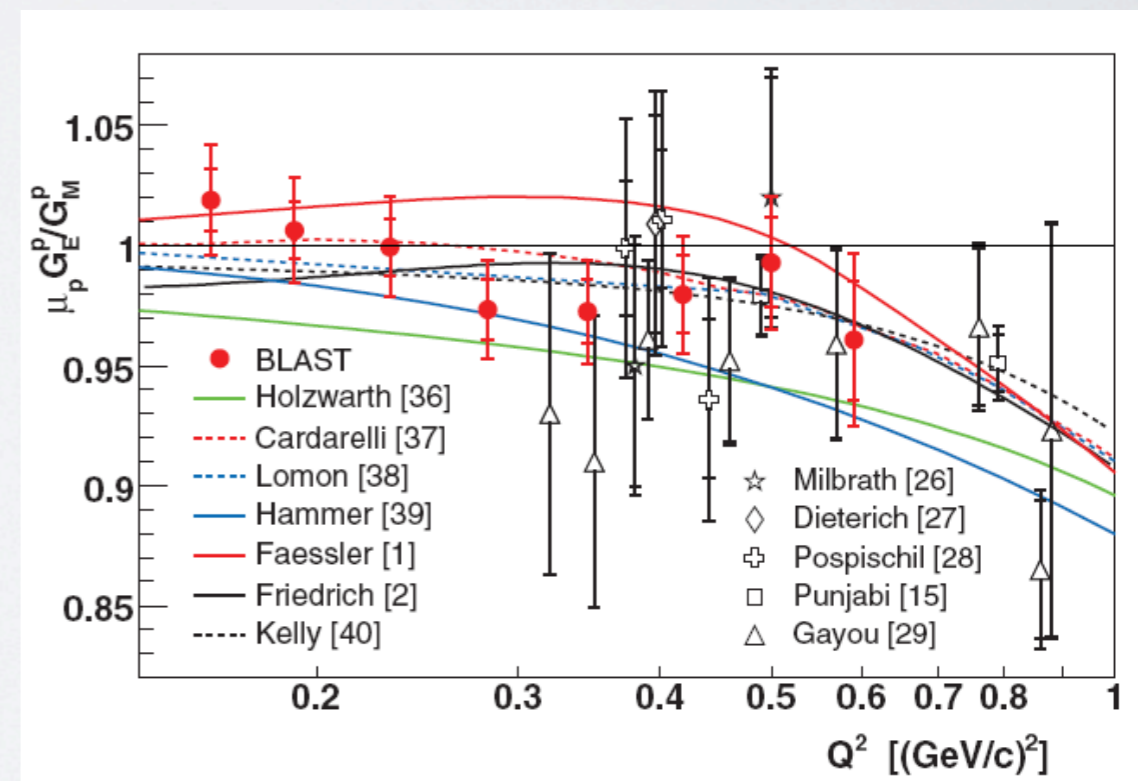
- Bump / dip (+2 dipoles) structure in all 4 form factors.
- Possibly interpreted as effects of a virtual meson cloud.



## BLAST @ MIT Bates - proton

*C.B. Crawford et al., Phys. Rev. Lett. 98, 052301 (2007)*

- Beam target asymmetry measurement using polarized H internal gas target.
- (Barely) consistent with unity and the F&W analysis.



# The JLab low $Q^2$ program

## Proton FFs

- LEDEX - Single arm proton measurement
  - Recoil polarization measurement of the FF ratio.
  - Calibration run from  $\gamma$ D measurement.
  - 8  $Q^2$  data points (0.25 - 0.5  $\text{GeV}^2$ ) with  $\sim 1.5\%$  uncertainty on best data points.
  - Led to the proposal of:

# The JLab low $Q^2$ program

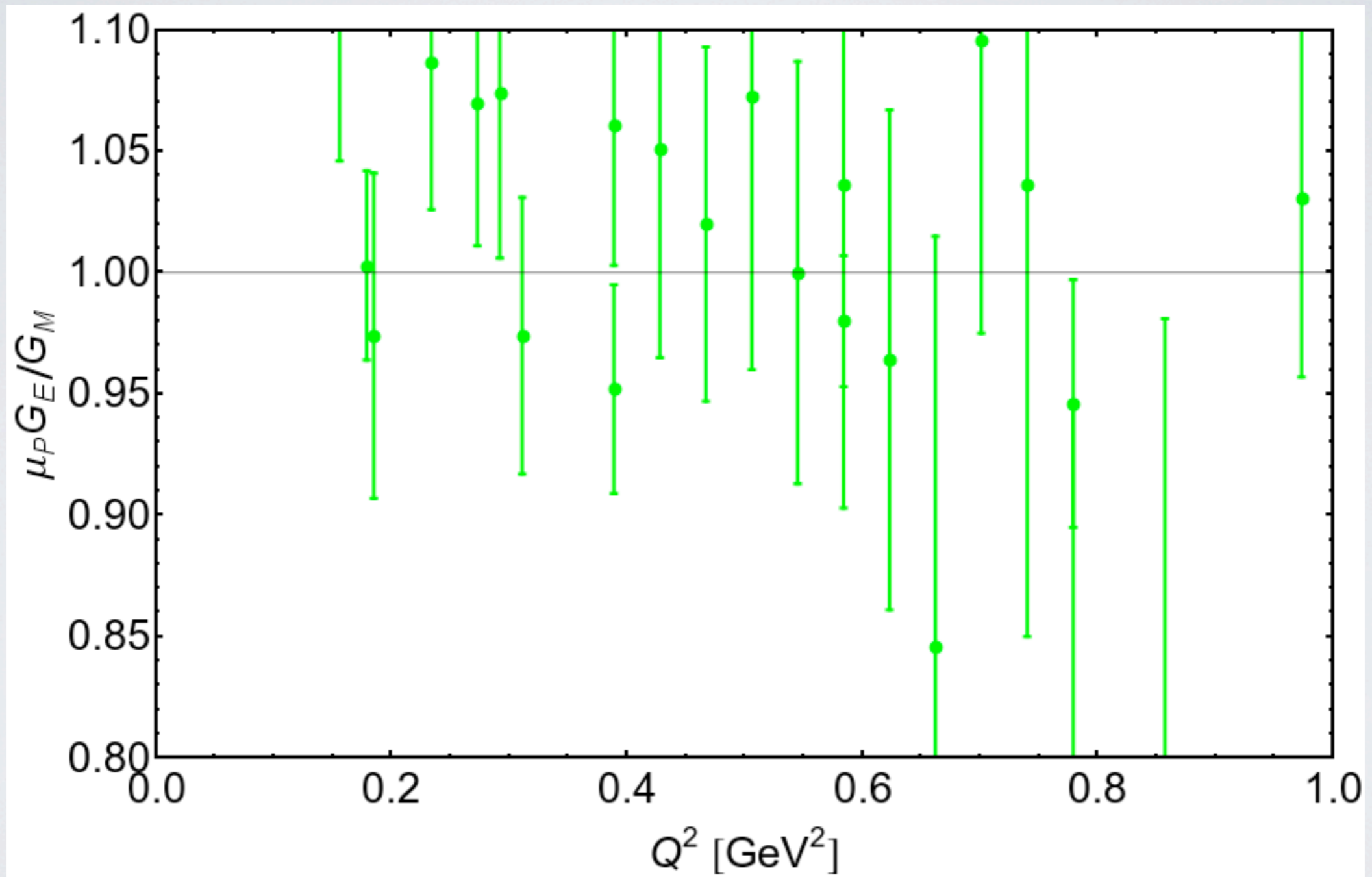
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  - Led to the proposal of:
- E08-007 - Two arm experiment (proton + tagged electron for bck suppression)
  - A dedicated 2 part experiment to map the proton FF ratio at low  $Q^2$ .
  - First part used recoil polarization to achieve:
    - $\sim 1\%$  uncertainty (*best ever achieved*) at  $Q^2 \sim 0.3 - 0.7 \text{ GeV}^2$ .
  - Second part will use beam target asymmetry (more later).



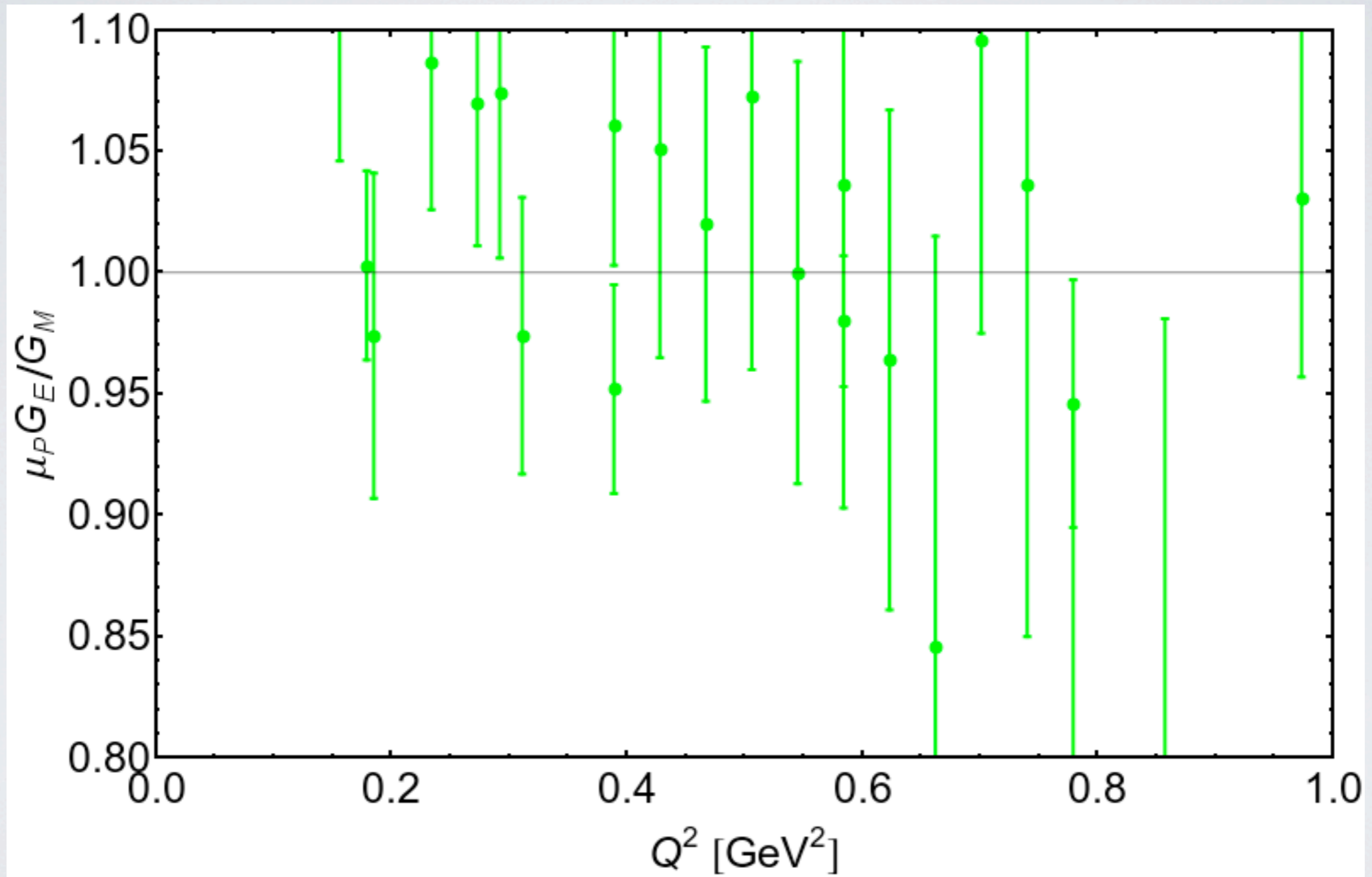
# A Sense of Scale

## Rosenbluth



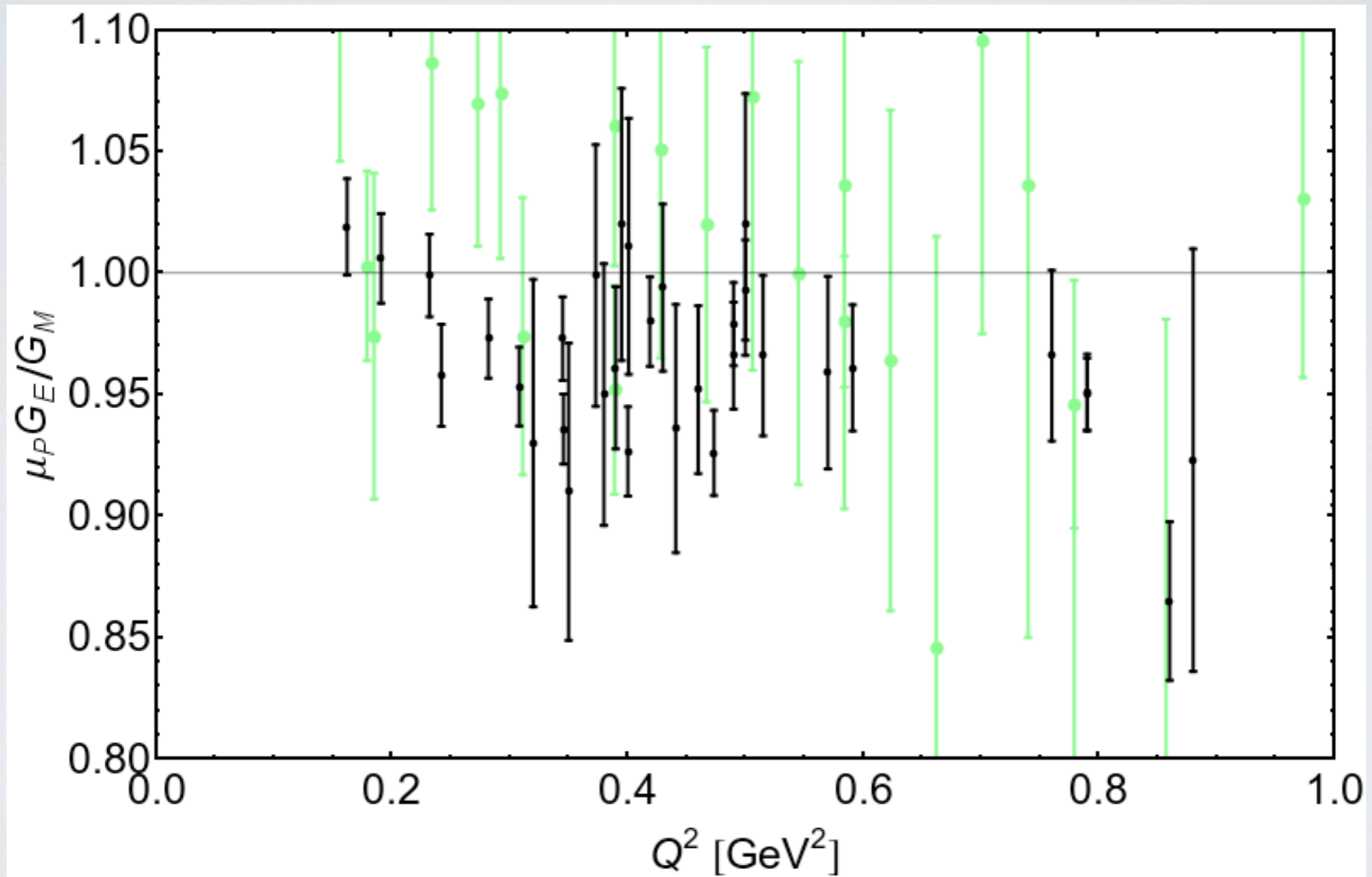
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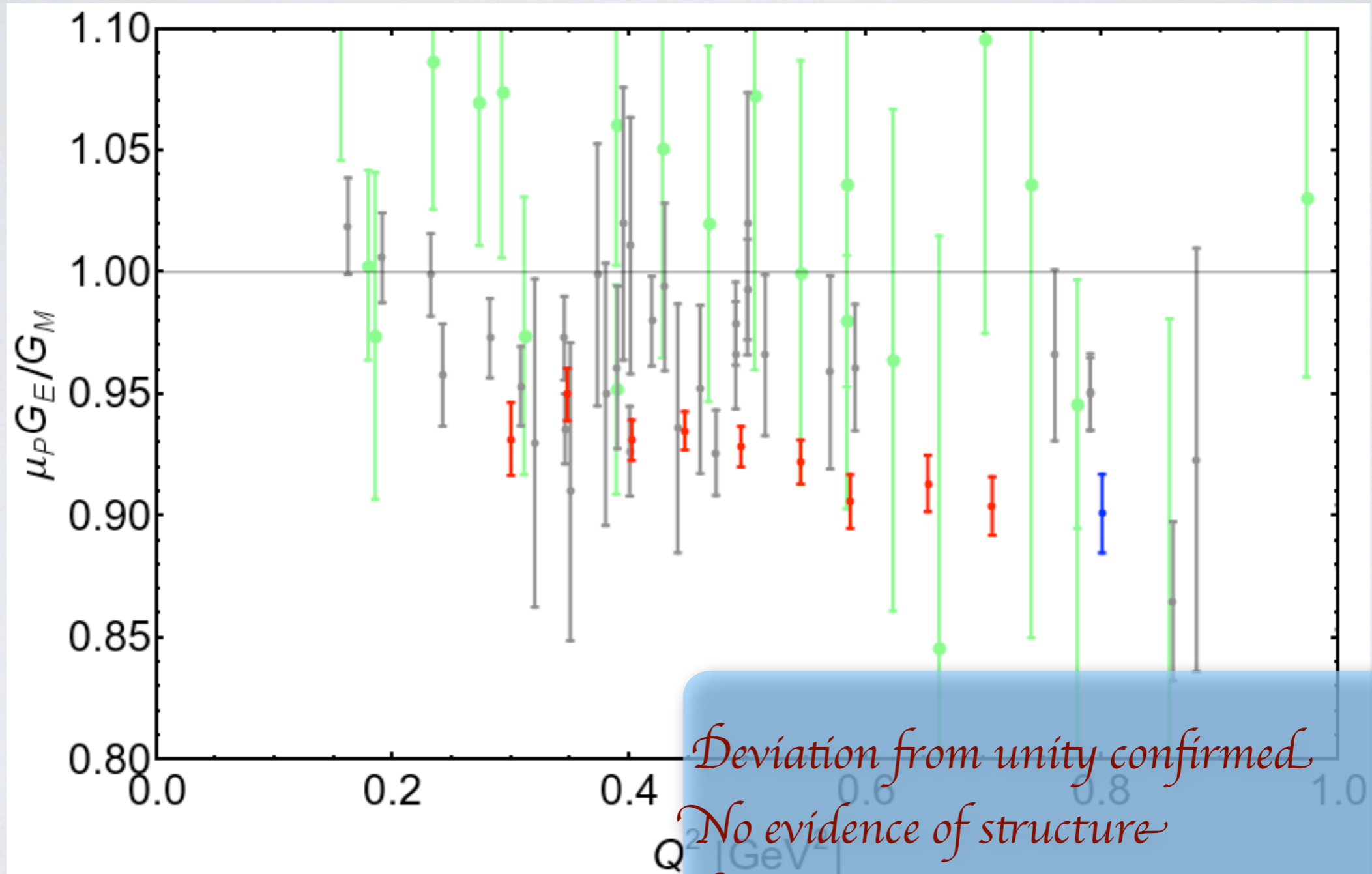
## World Polarization Data



# A Sense of Scale

## E08007 - Part I

(and E03-104)



*Deviation from unity confirmed*

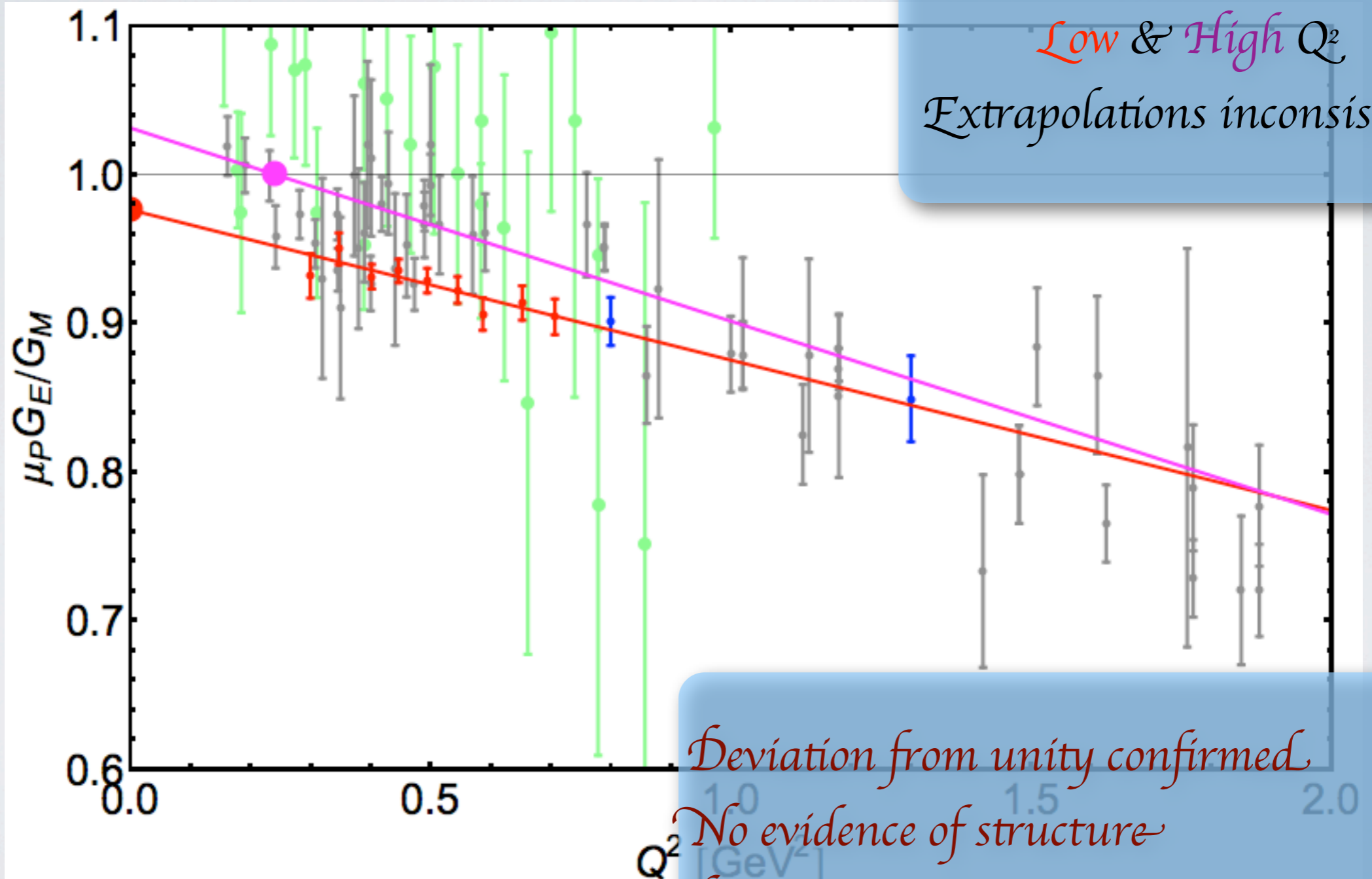
*No evidence of structure*

*Relativistic effects important even at low  $Q^2$*

# A Sense of Scale

E08007 - Part I

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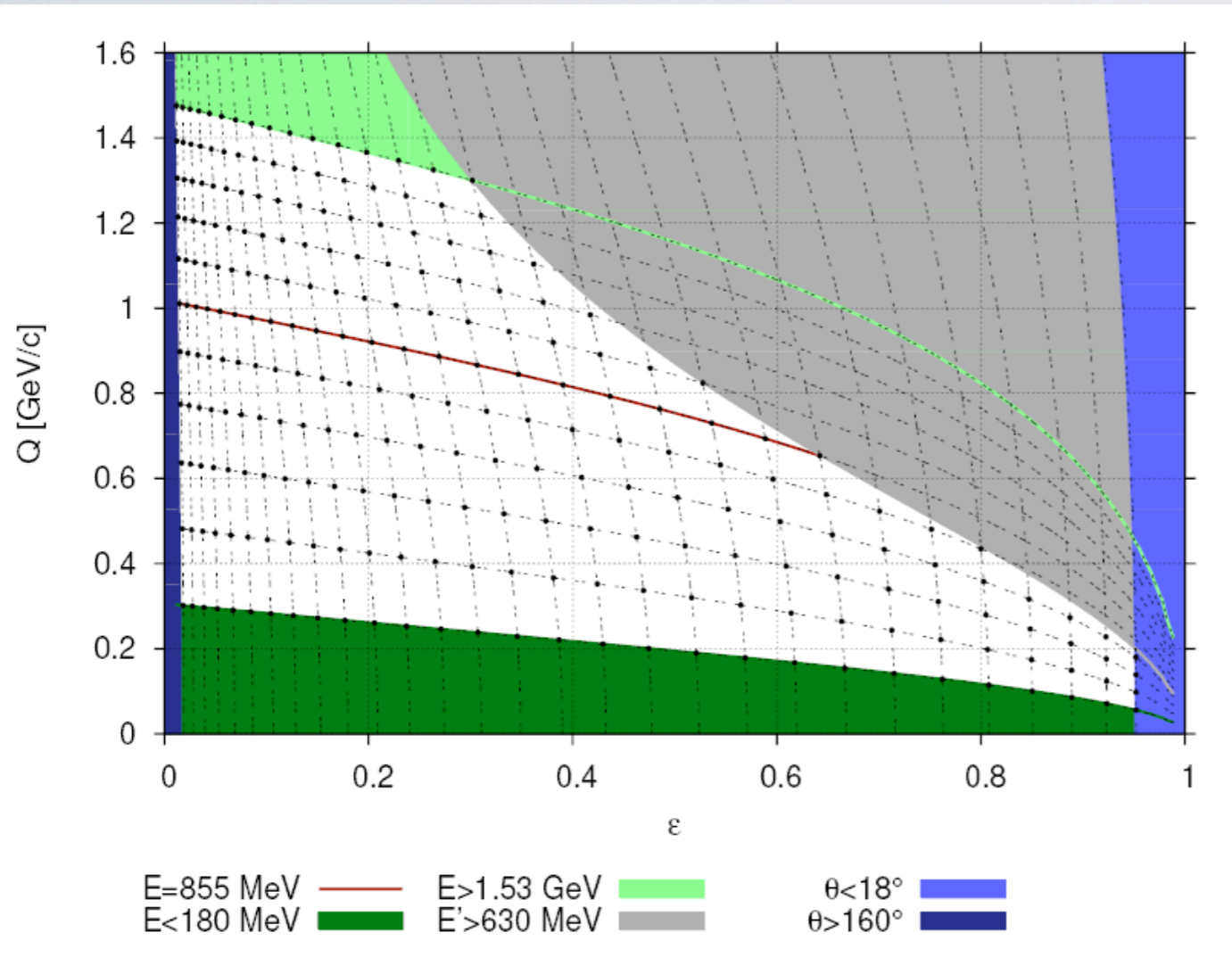


*Low & High  $Q^2$*   
*Extrapolations inconsistent.*

*Deviation from unity confirmed.*  
*No evidence of structure*  
*Relativistic effects important even at low  $Q^2$*

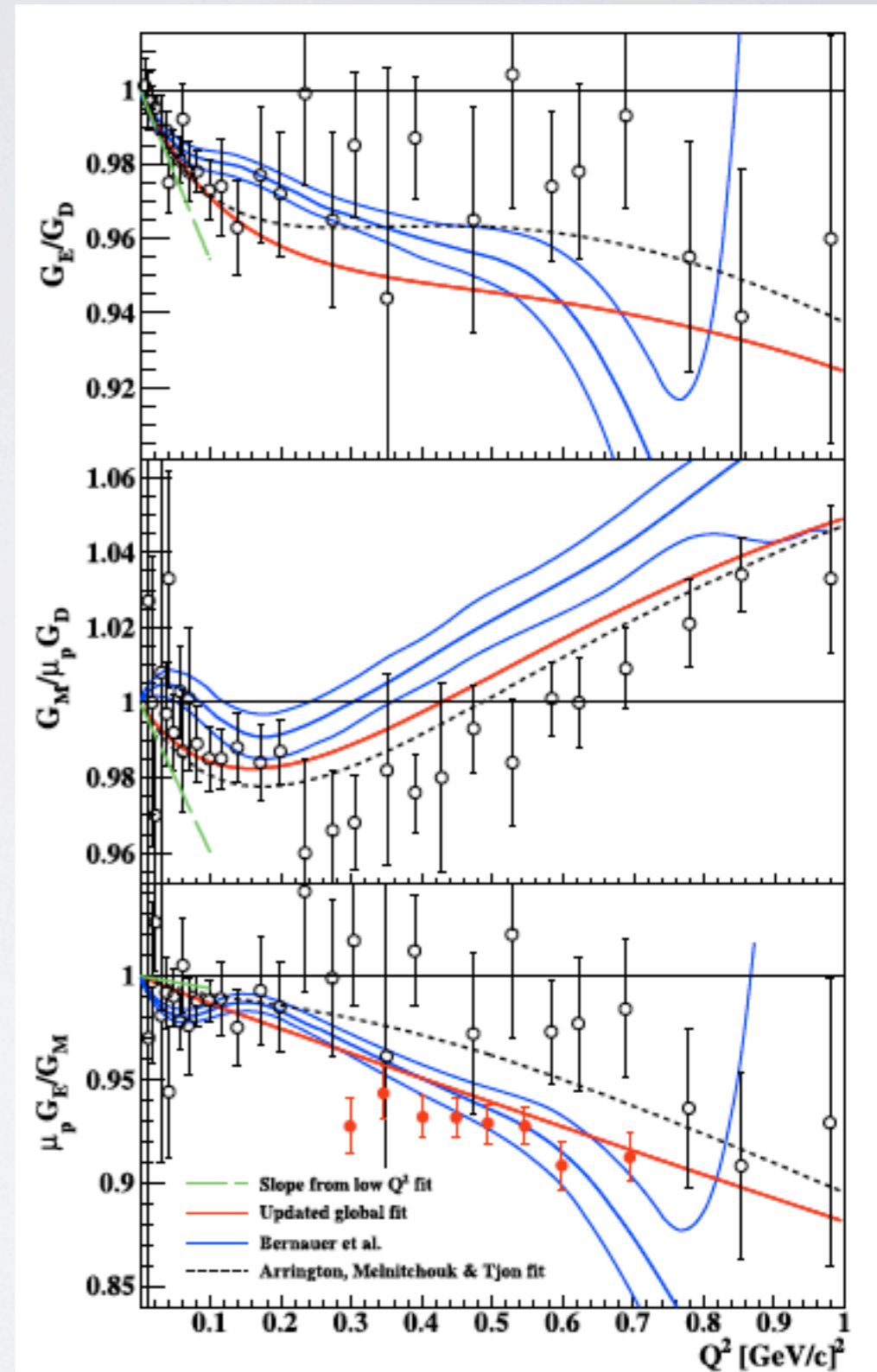
# MAINZ A1 MEASUREMENT

## High precision low $Q^2$



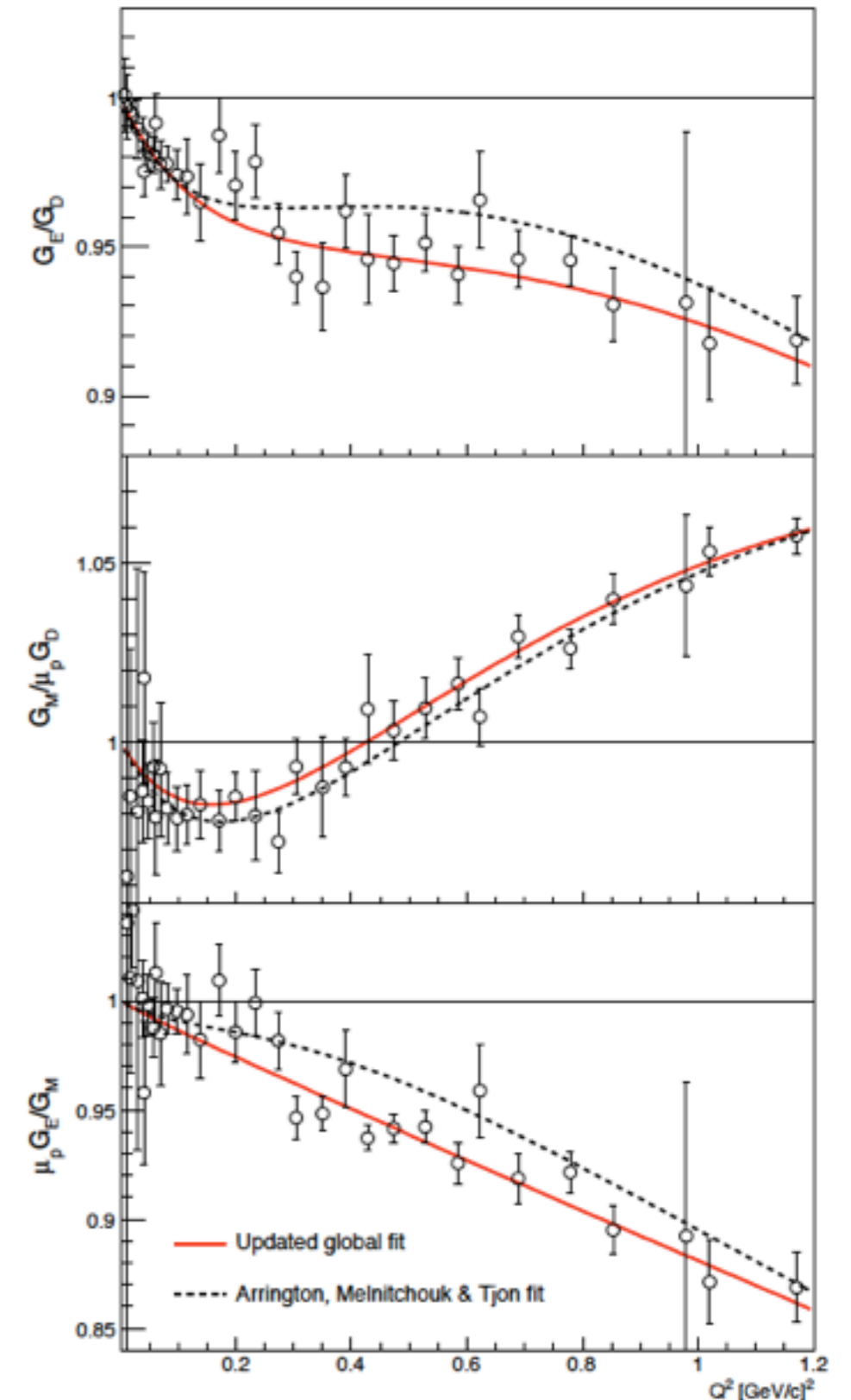
$$\langle r_E^2 \rangle^{\frac{1}{2}} = 0.879(5)_{\text{stat.}}(4)_{\text{syst.}}(2)_{\text{model}}(4)_{\text{group}} \text{ fm},$$

$$\langle r_M^2 \rangle^{\frac{1}{2}} = 0.777(13)_{\text{stat.}}(9)_{\text{syst.}}(5)_{\text{model}}(2)_{\text{group}} \text{ fm}.$$



# What we've learned - Recent Fits

- Plots compare (2007) AMT fit to **fit using newest data**.
- New fits reduce  $G_E$  by  $\sim 2\%$ .
- Slope as  $Q^2 \rightarrow 0$  changed (impacts radii).



# Extracting the individual FFs

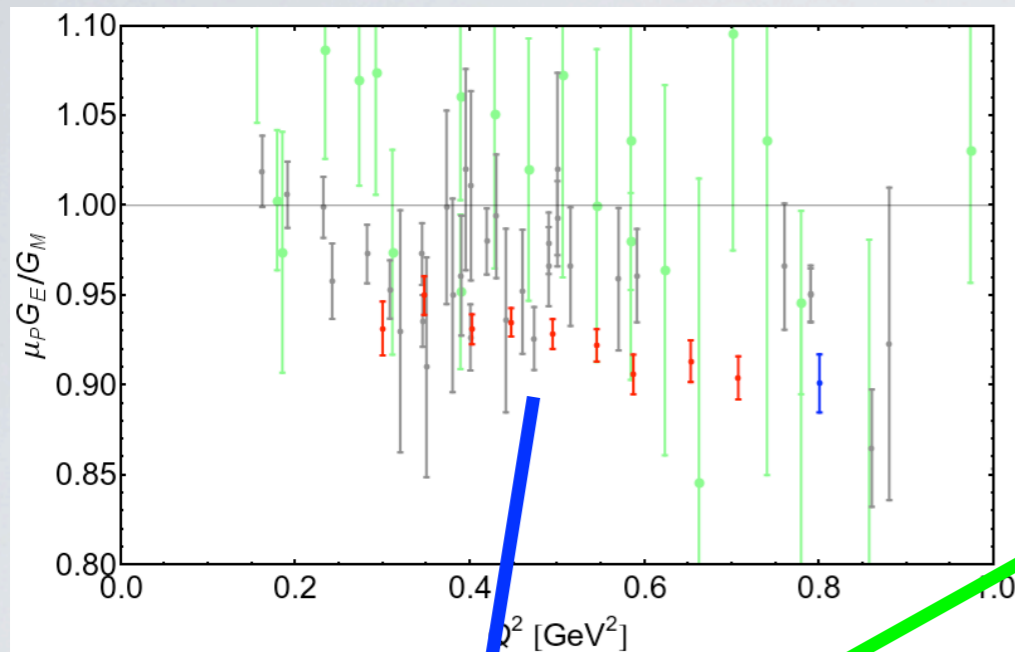
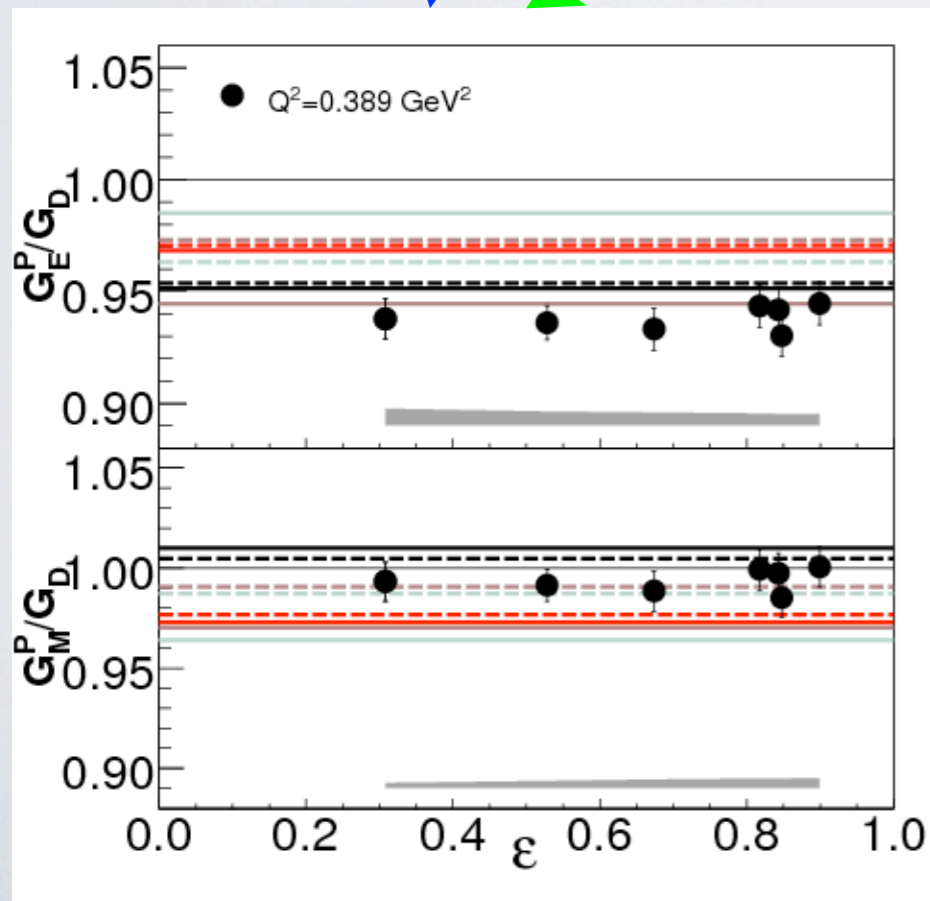


Table 1.  
Differential cross sections: The quoted errors are only random errors. A normalization error of  $\pm 4\%$  has to be added.

$q^2$ ( $\text{GeV}^2$ )	$\theta$ ( $^\circ$ )	$s_0$ (GeV)	$\frac{d\sigma}{d\Omega}$ [ $10^{-34} \frac{\text{cm}^2}{\text{ster}}$ ]	
2	25.25	0.660	32800	$\pm 990$
3	25.25	0.815	18570	$\pm 550$
3,065	35.15	0.605	8630	$\pm 260$
5	25.25	1.064	8410	$\pm 260$
	35.15	0.784	4000	$\pm 120$
8	25.25	1.364	3610	$\pm 90$
10	25.25	1.537	2285	$\pm 46$
	31.74	1.249	1328	$\pm 26$
	32.27	1.231	1310	$\pm 26$
	35.15	1.142	1080	$\pm 22$
	50.06	0.848	460.3	$\pm 9.4$
	64.72	0.696	252.9	$\pm 4.1$
	90.27	0.556	117.8	$\pm 2.3$



High precision cross section and FFR combined  $\rightarrow$  High precision individual form factors.

Deviation from unity (at least for  $Q^2 \sim 0.39 \text{ GeV}^2$ ) caused by  $G_E$ .

Will eventually combine with high precision Mainz XS database.

*G. Ron et al., Phys. Rev. Lett. 99, 202002 (2007)*



# What we've learned

## Charge Densities

- Sachs FFs cannot be related to charge/magnetization densities:
- Relativistic effects (Lorentz contraction).
- Initial/Final states not identical (cannot be interpreted as density).
- Can be shown that  $F_1$  &  $F_2$  are 2D transforms of charge and magnetization densities.
- Low  $Q^2$  expansion gives:

$$\langle b^2 \rangle_M - \langle b^2 \rangle_{Ch} = \frac{\mu}{\kappa} \frac{2}{3} (R_M^{*2} - R_E^{*2}) + \frac{\mu}{M^2}$$

- And fit to data gives:

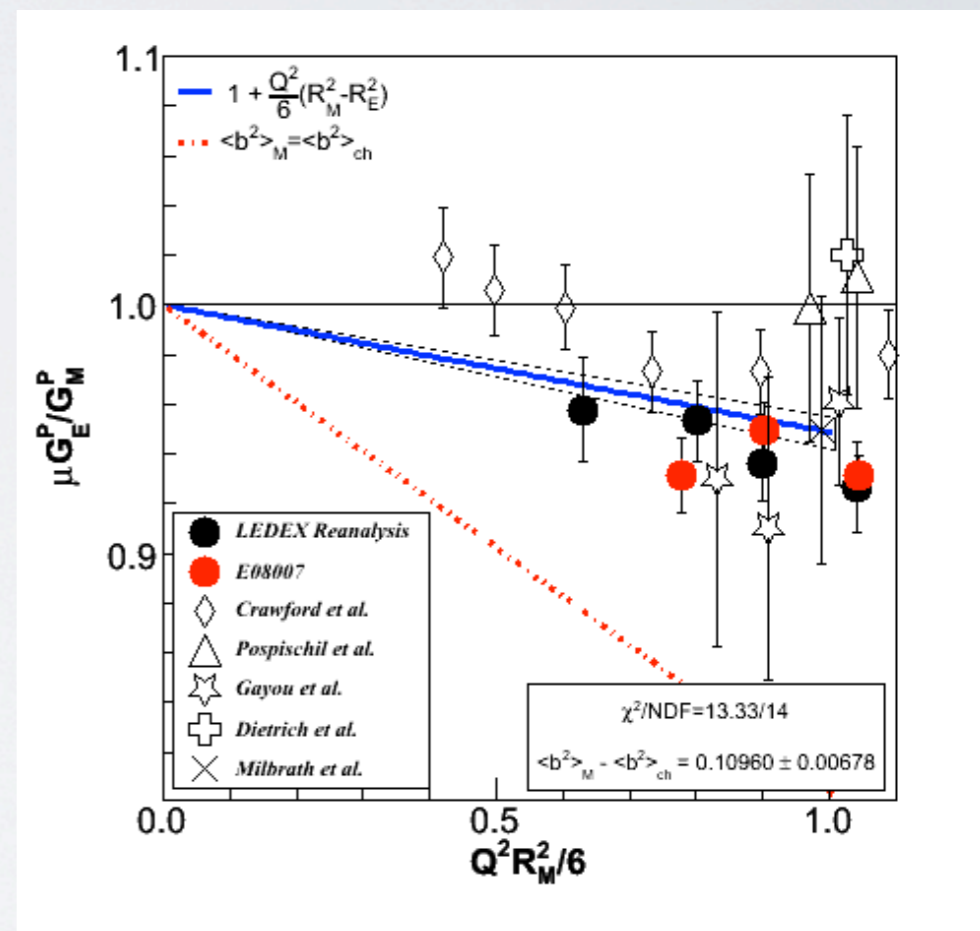
$$\langle b^2 \rangle_M - \langle b^2 \rangle_{ch} = 0.0909 \pm 0.0039 \text{ fm}^2$$

*G. Miller, Phys. Rev. Lett. 99, 112001 (2007)*

*G. Miller, E. Piasezky & G. Ron, Phys. Rev. Lett. 101, 082002 (2008)*

$$\rho_{Ch}(\vec{b}) = \mathcal{F}^{-1} [F_1(Q^2)]$$

$$\rho_M(\vec{b}) = \mathcal{F}^{-1} [F_2(Q^2)]$$



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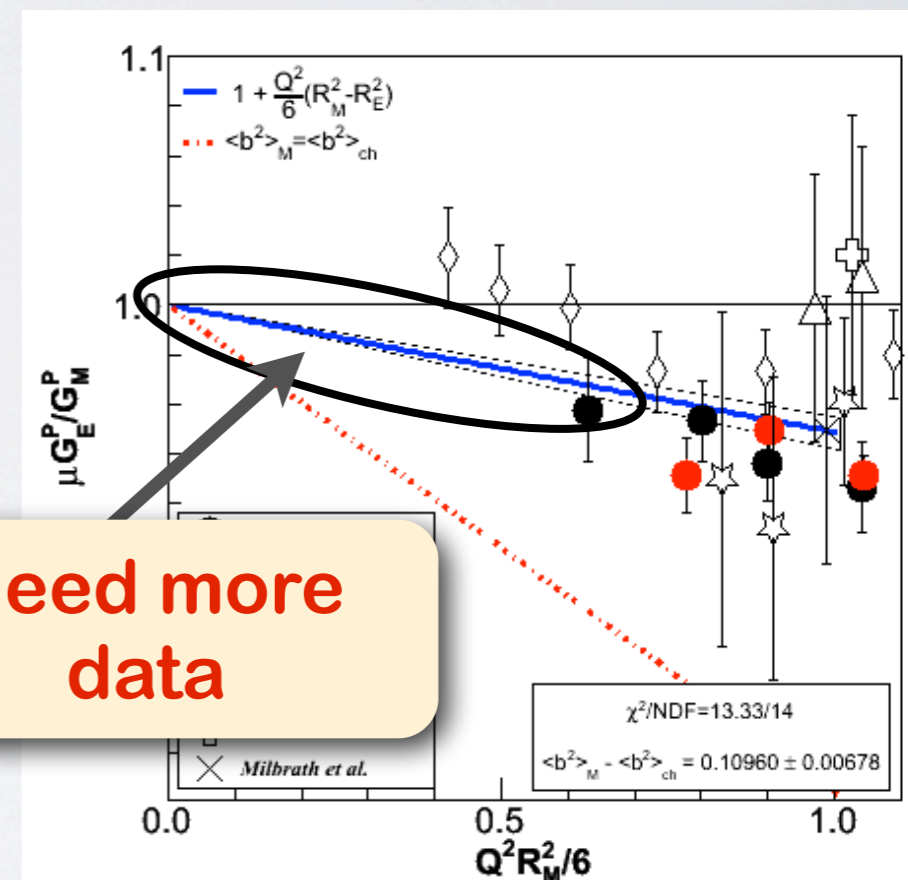
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**Need more data**

# What we've learned

## Charge Densities

• *Actually needs to be modified.  
But overall conclusion stays.*

- Relativistic effects (Lorentz contraction).
- Initial/Final states not identical (cannot be interpreted as density).
- Can be shown that  $F_1$  &  $F_2$  are 2D transforms of charge and magnetization densities.
- Low  $Q^2$  expansion gives:

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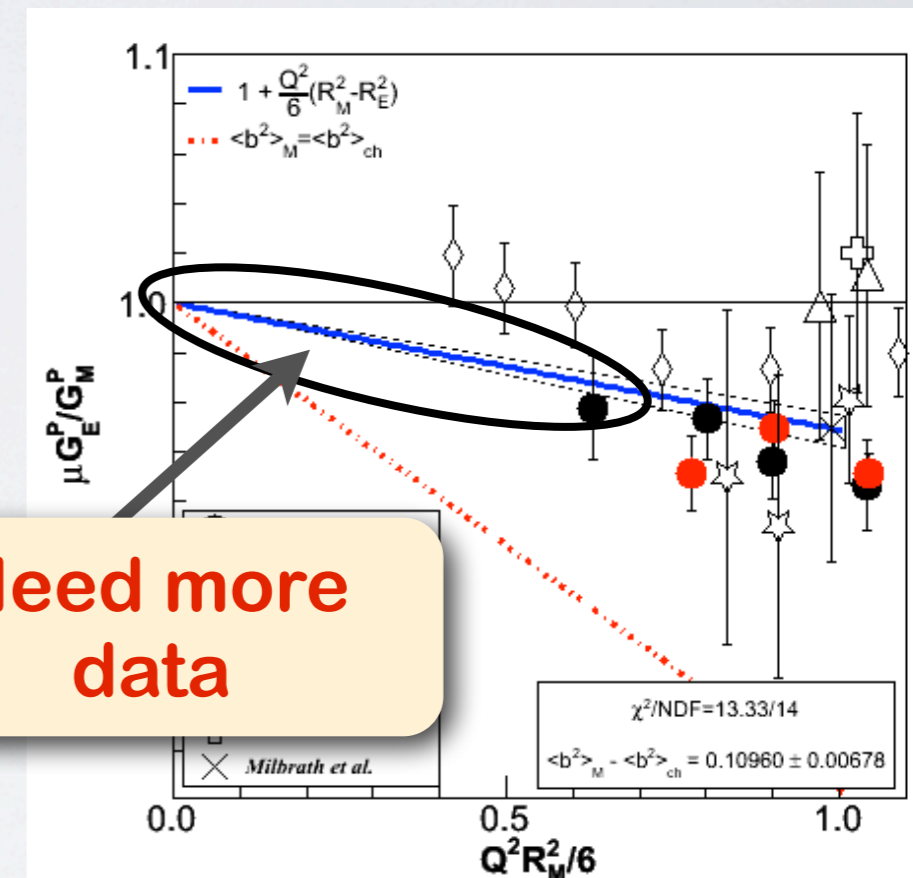
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**Need more data**

# The Proton Radius

A multitude of extractions

- Low  $Q^2$  Expansion of

$G_E$ :

$$G_E^P(Q^2) \sim 1 = 1 - \frac{q^2 \langle r^2 \rangle}{6} + \dots$$

- Lattice QCD in the chiral limit.
- Hydrogen Lamb shift.
- Muonic Hydrogen Lamb shift.

# The Proton Radius

## A multitude of extractions

- Low  $Q^2$  Expansion of

$G_E$ :

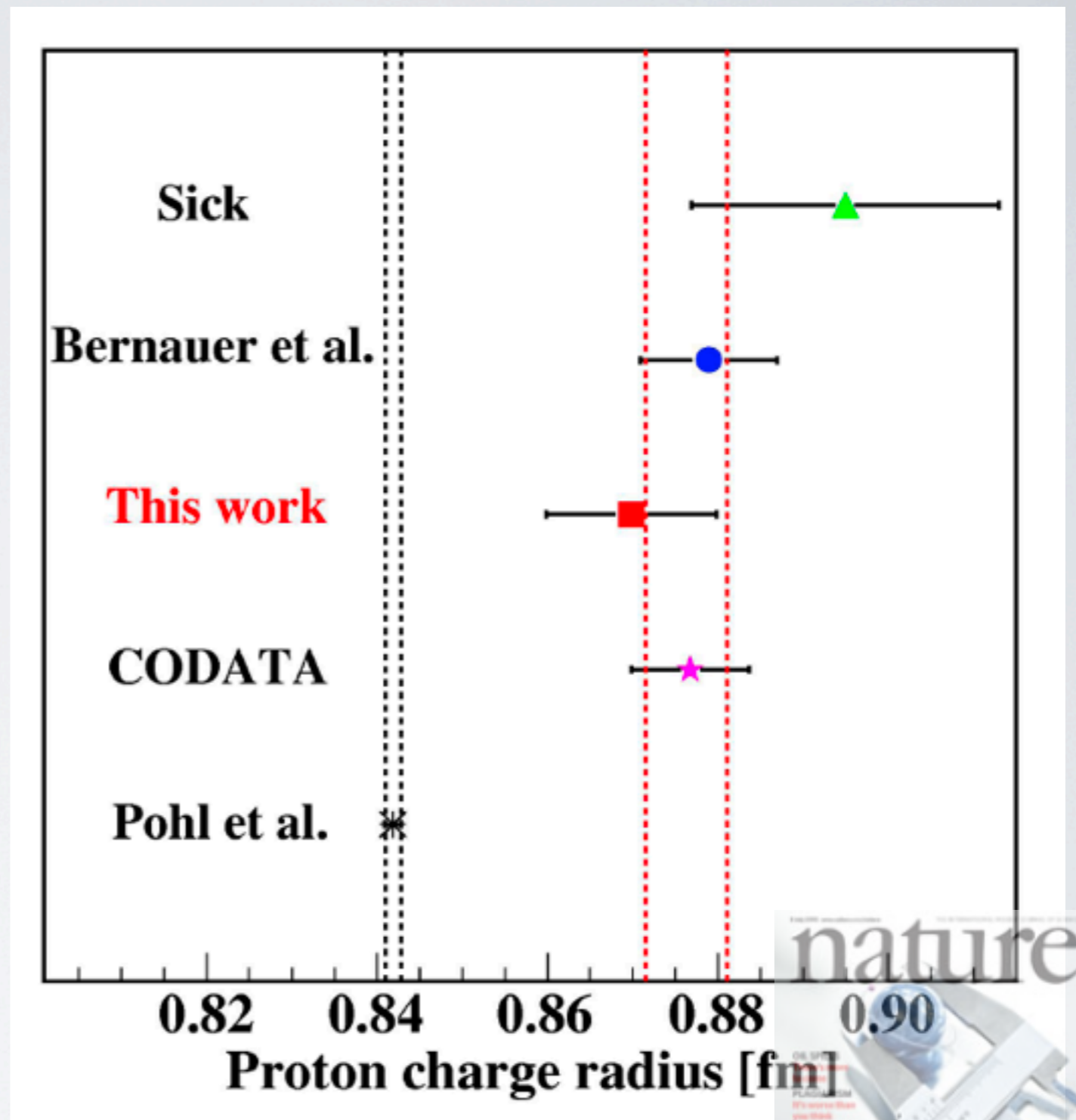
$$G_E^P(Q^2) \sim 1 = 1 - \frac{q^2 \langle r^2 \rangle}{6} + \dots$$

- Lattice QCD in the chiral limit.
- Hydrogen Lamb shift.
- Muonic Hydrogen Lamb shift.

- Sensitive to functional form chosen for  $G_E$ . Also, data at  $Q^2 \sim 0$  scarce (non-existent).
- Sensitive to lattice size and small perturbations in parameters.
- Sensitive to different theoretical corrections.

# The Proton Radius Puzzle

#	Extraction	$\langle r_E \rangle^2$ [fm]
1	Sick	$0.895 \pm 0.018$
2	CODATA	$0.8768 \pm 0.0069$
3	Mainz	$0.879 \pm 0.008$
4	This Work	$0.870 \pm 0.010$
5	Combined 2-4	$0.8764 \pm 0.0047$
6	Muonic Hydrogen	$0.842 \pm 0.001$



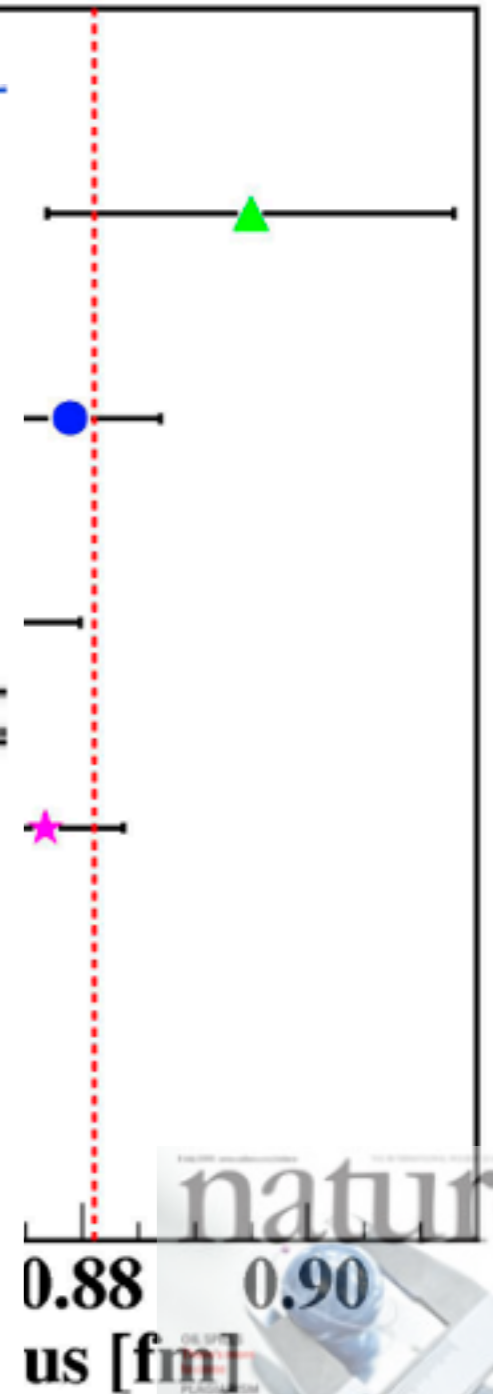
# The Proton Radius Puzzle

#	Extraction
1	Sick
2	CODATA
3	Mainz
4	This Work
5	Combined 2-4
6	Muonic Hydrogen



"I don't have time to write performance reviews, so I'll just criticize you in public from time to time."

0.0 1.0 2.0 3.0



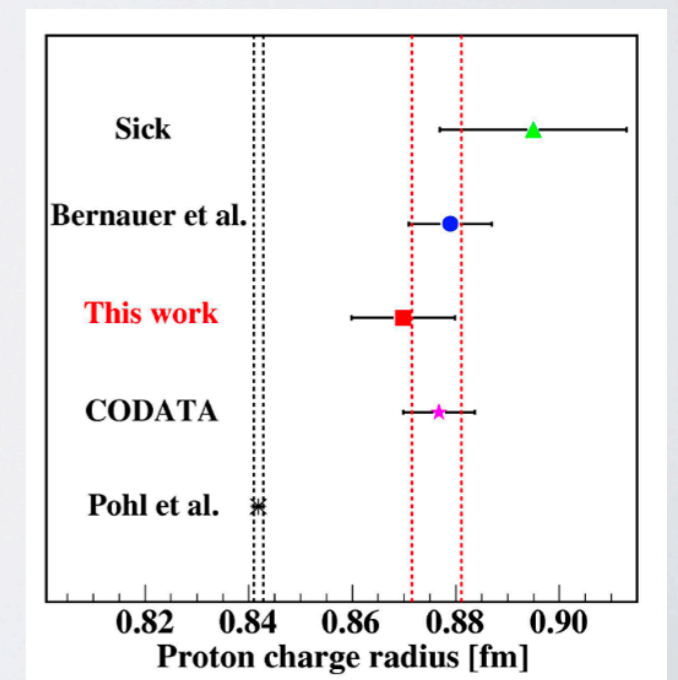
# The Proton Radius Puzzle

## My Caveats

- Sachs form factors not measured at  $Q^2 = 0$ .
- Can we even extrapolate Sachs form factors to  $Q^2$  and claim that we get the radius? **Extrapolation from relativistic to non-relativistic region.**
- Mainz data extracted with no 2-photon corrections (and get a strange magnetic radius).
- **Electron scattering results agree well with CODATA (Lamb shift) - seems to indicate electron/muon discrepancy.**

## My wishlist

- E08007-II to measure very low  $Q^2$  form factors.
- Possible other experiments at low  $Q^2$  (Proton scattering off atomic hydrogen?  $\mu p$  scattering experiment?).
- Another theoretical look at the derivation from muonic Lamb shift.
- Comparison of (as yet unreleased) Zemach radius data from PSI.





# The Zemach Radius

- Hyperfine splitting of the hydrogen ground state:

$$E_{hfs}(e^- p) = (1 + \Delta_{QED} + \Delta_R^P + \Delta_{h\nu p}^P + \Delta_{\mu\nu p}^P + \Delta_{weak}^P + \Delta_S) E_F^P$$

$$\Delta_S = \Delta_Z + \Delta_{pol}, \quad \Delta_Z = -2\alpha m_e r_Z (1 + \delta_Z^{rad})$$

- Zemach radius (effect of proton internal structure on energy level shift):

$$r_Z = -\frac{4}{\pi} \int_0^\infty \frac{dQ}{Q^2} \left[ G_E(Q^2) \frac{G_M(Q^2)}{1 + \kappa_P} - 1 \right]$$

- Sensitivity to details in the FFs is completely contained in the  $Q^2 < 1 \text{ GeV}^2$  region.
- Leading theoretical uncertainty in one of the most precisely measured experimental quantities (test of QED).

FF	$r_p$ [fm]	$r_Z$ [fm]	$\Delta Z$ [ppm]
AMT	0.885	1.080	-41.43
AS	0.879	1.091	-41.85
Kelly	0.878	1.069	-40.99
F&W	0.808	1.049	-40.22
Dipole	0.851	1.025	-39.29
New	0.868	1.075	-41.22

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$$\Delta_S = \Delta_Z + \Delta_{rel\ shift}$$

Note that using different parametrizations results in deviations larger than quoted uncertainty!

- Zemach radius

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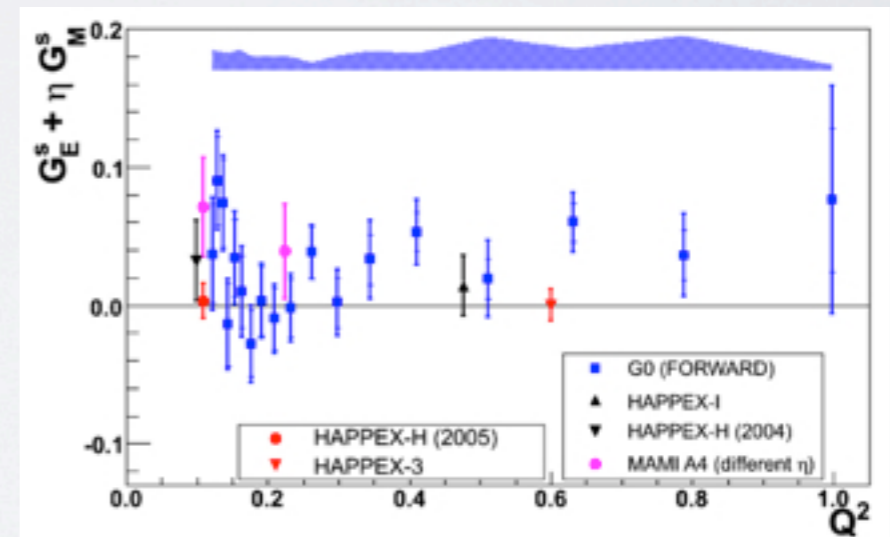
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# PV Experiments

- Parity violation experiments aim to measure the strange quark content of the nucleon by detecting interference between elastic EM scattering and neutral weak ep scattering.
- Determination of strange quark form factors relies on knowledge of EMFF.
- Shifts of  $\sim 0.5\sigma$  “easy”.

$Q^2$	$\Delta A/\sigma$	$\Delta A/A$	
0.38	0.42	1.6%	GO FWD
0.56	0.50	1.6%	GO FWD
1.0	0.30	0.8%	GO FWD
0.50	0.50	1.7%	HappexII
0.231	0.12	0.2%	GO BCK
0.65	0.14	0.3%	GO BCK



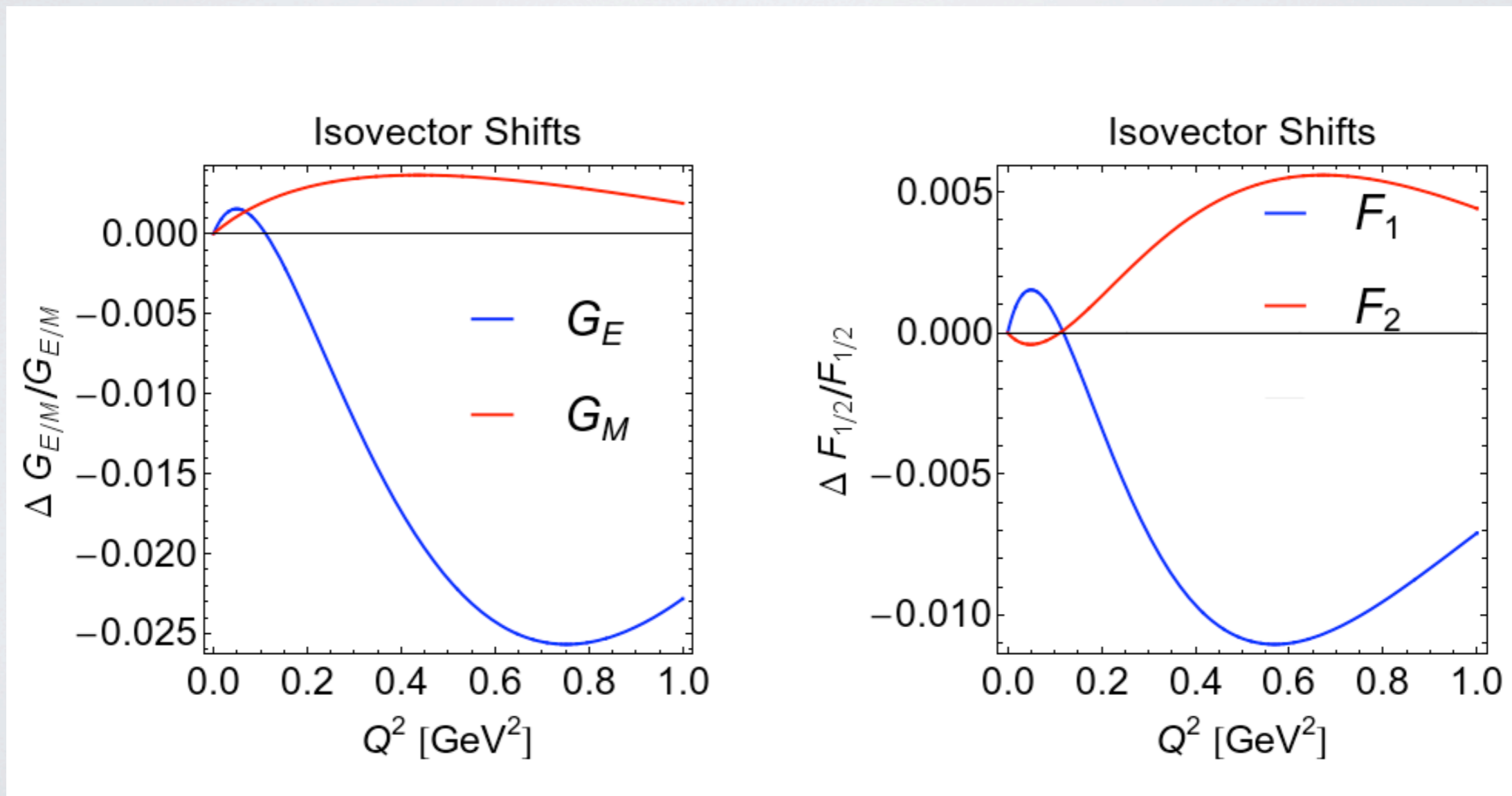
$$A^{PV} = \left[ -\frac{G_F M_p^2 Q^2}{\pi \alpha \sqrt{2}} \right] \left[ (1 - 4 \sin^2 \theta_W) - \frac{\varepsilon G_E^{p\gamma} (G_E^{n\gamma} + G_E^s) + \tau G_E^{p\gamma} (G_M^{n\gamma} + G_M^s)}{\varepsilon (G_E^{p\gamma})^2 + \tau (G_M^{p\gamma})^2} \right] - A_A$$

# Isovector / Isoscalar Separation

Reminder:  $IV=p-n$ ,  $IS=p+n$

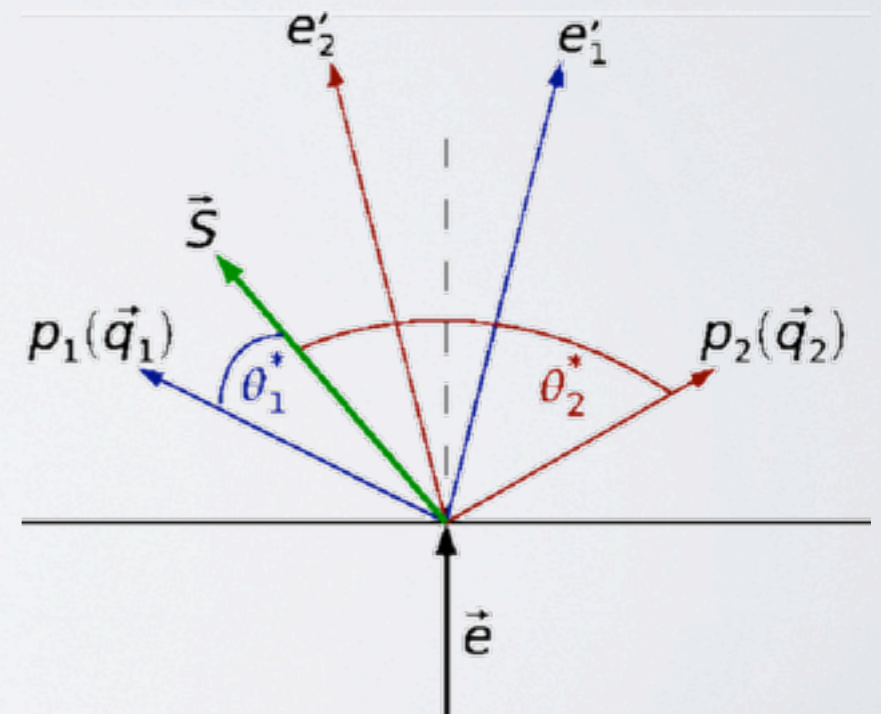
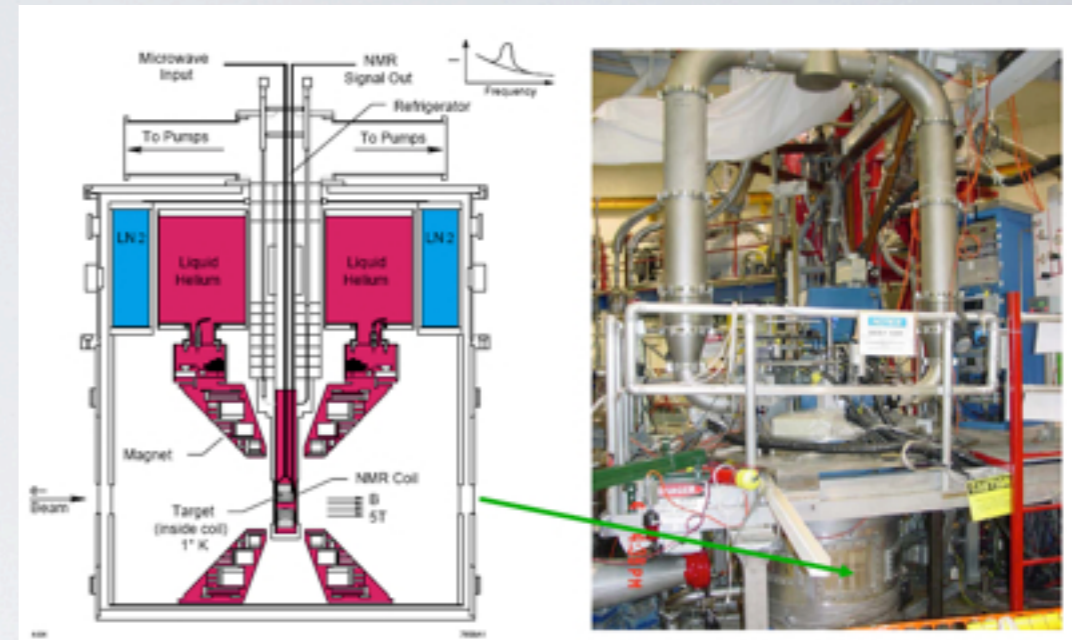
Important for Lattice QCD (Isovector)

Plot shows the fractional change in the isovector form factors when using J. Arrington's new vs. old parametrizations (for the proton).



# E08007 - Part II

- High precision ( $< 1\%$ ) survey of the FF ratio at  $Q^2=0.01 - 0.16 \text{ GeV}^2$ .
- Beam-target asymmetry measurement by electron scattering from polarized  $\text{NH}_3$  target.
- Electrons detected in two **matched spectrometers**.
- Ratio of asymmetries cancels systematic errors  $\rightarrow$  **only one target setting to get FF ratio**.
- Designed to overlap E08007-I and Bates BLAST- **but magnet issues kill that**.
- Scheduled for Dec 2011 / Jan 2012 (**but delayed till Feb 2012!**)



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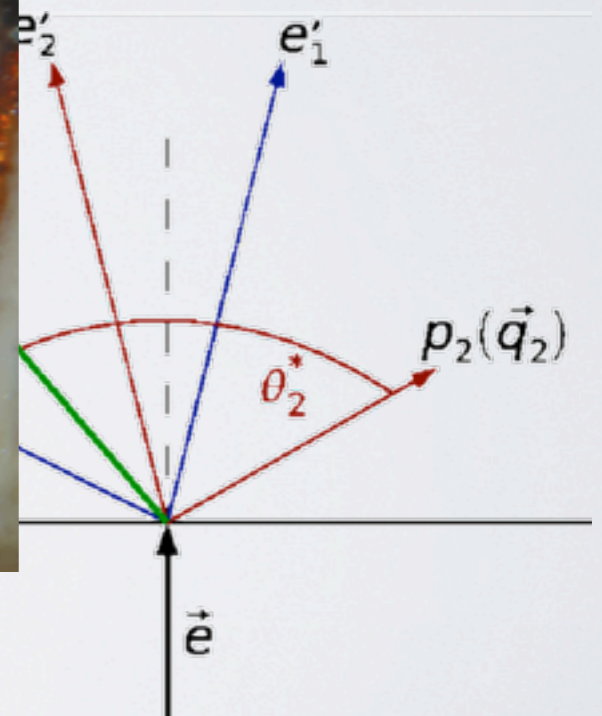
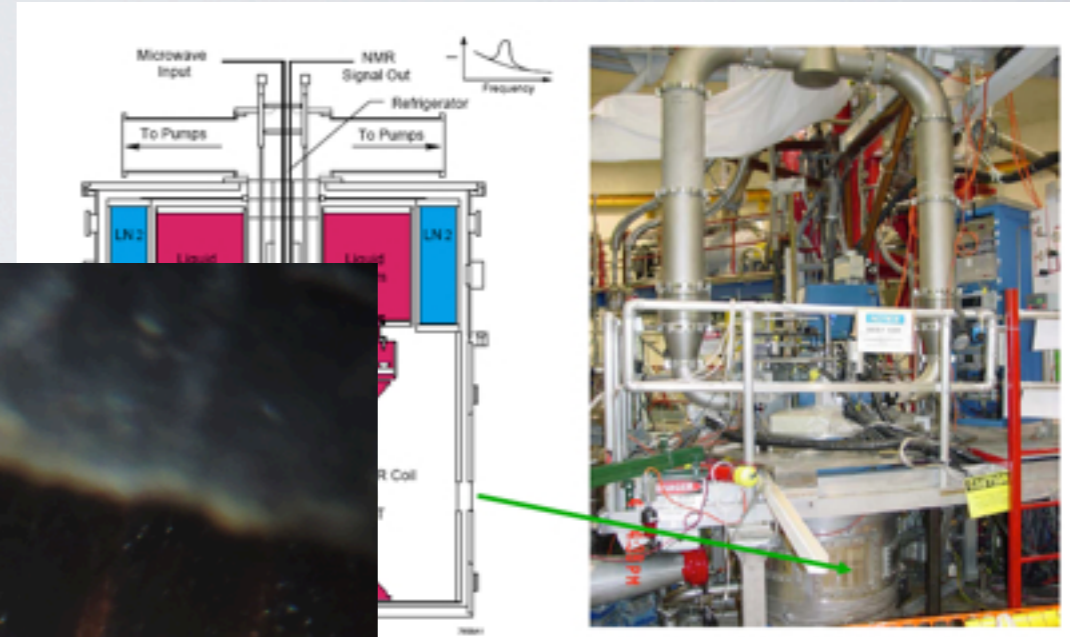
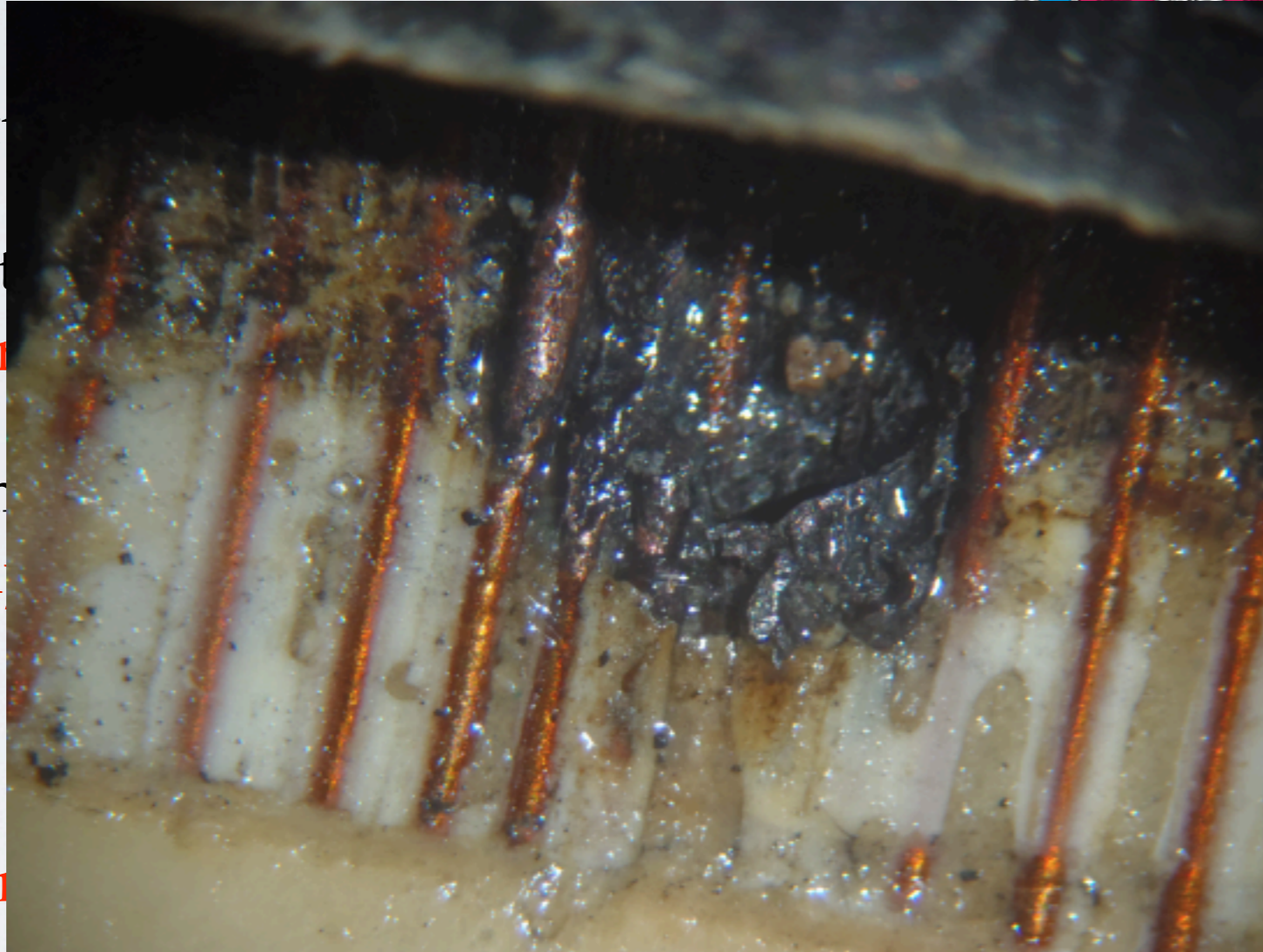
- Beam-target  
electron scattering

- Electrons detected by  
**spectrometer**

- Ratio of asymmetries  
errors  $\rightarrow$  **only ratio**.

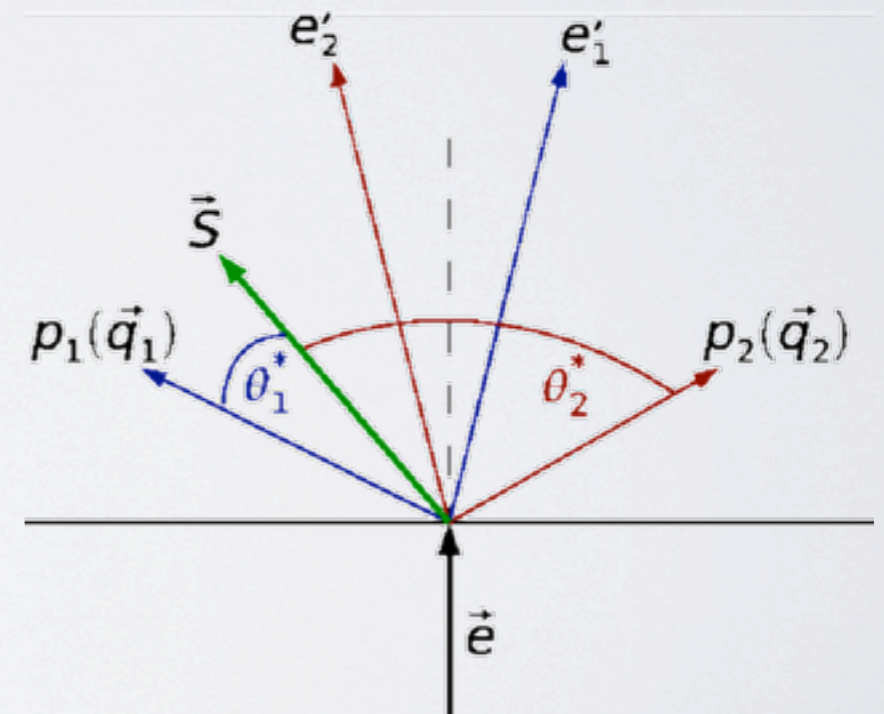
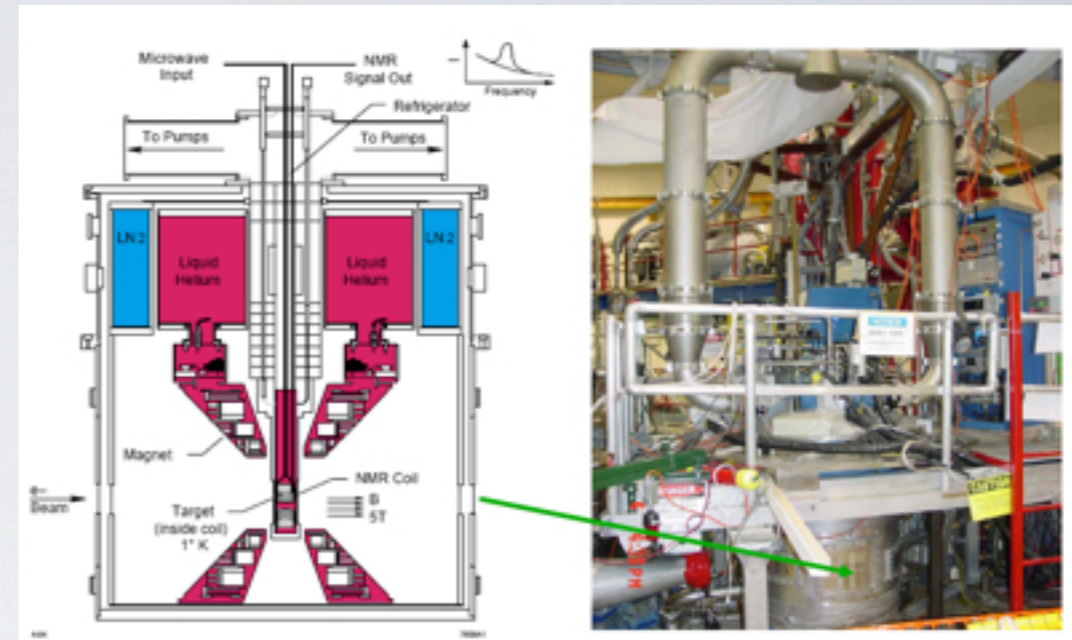
- Designed to be like  
BLAST- **but not**

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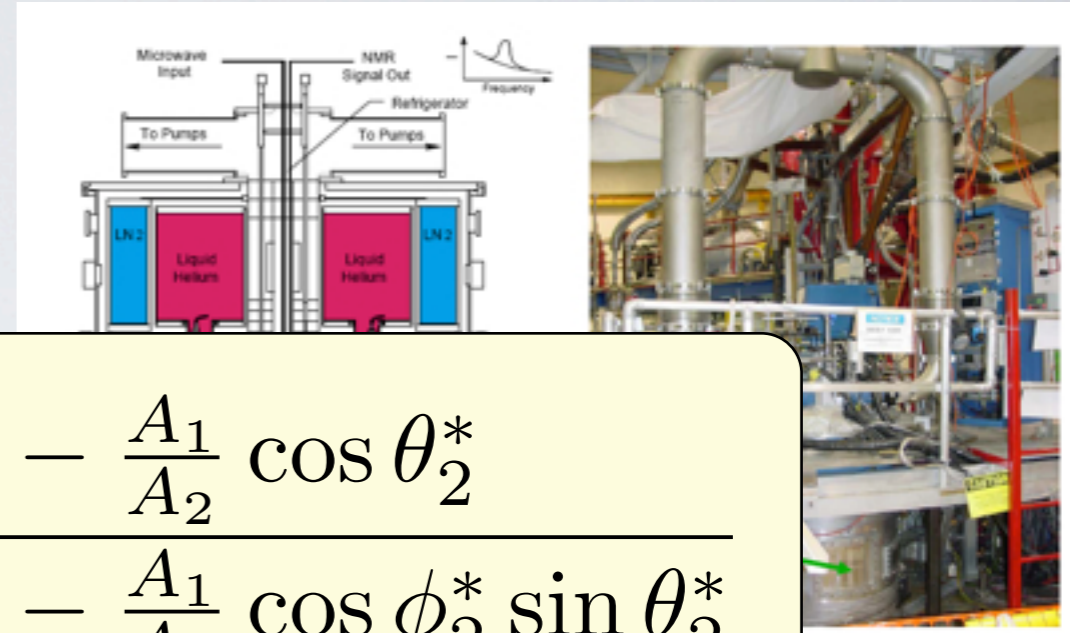
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- Beam-target asymmetry measurement by

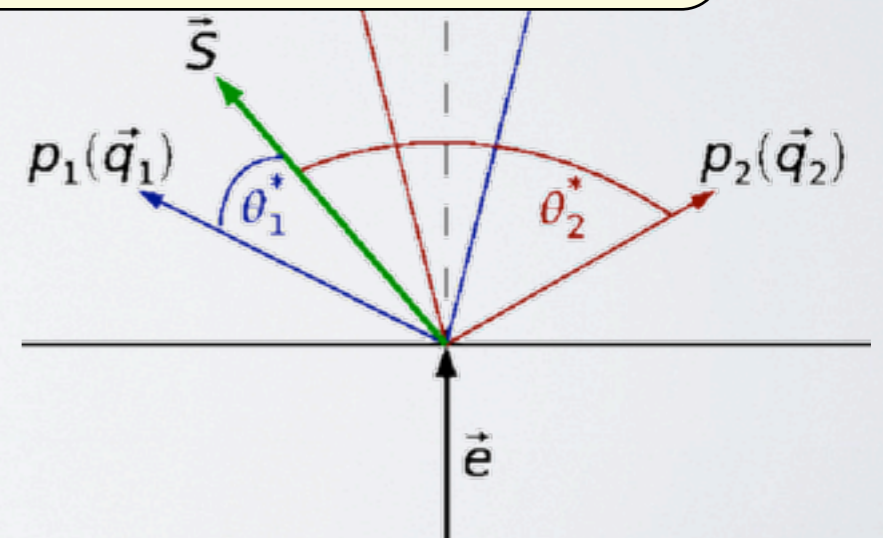
$$\mu_p \frac{G_E^p}{G_M^p} = -\mu_p a(\tau\theta) \frac{\cos \theta_1^* - \frac{A_1}{A_2} \cos \theta_2^*}{\cos \phi_1^* \sin \theta_1^* - \frac{A_1}{A_2} \cos \phi_2^* \sin \theta_2^*}$$

Note no dependence on polarizations/dilution

- Ratio error ratio.

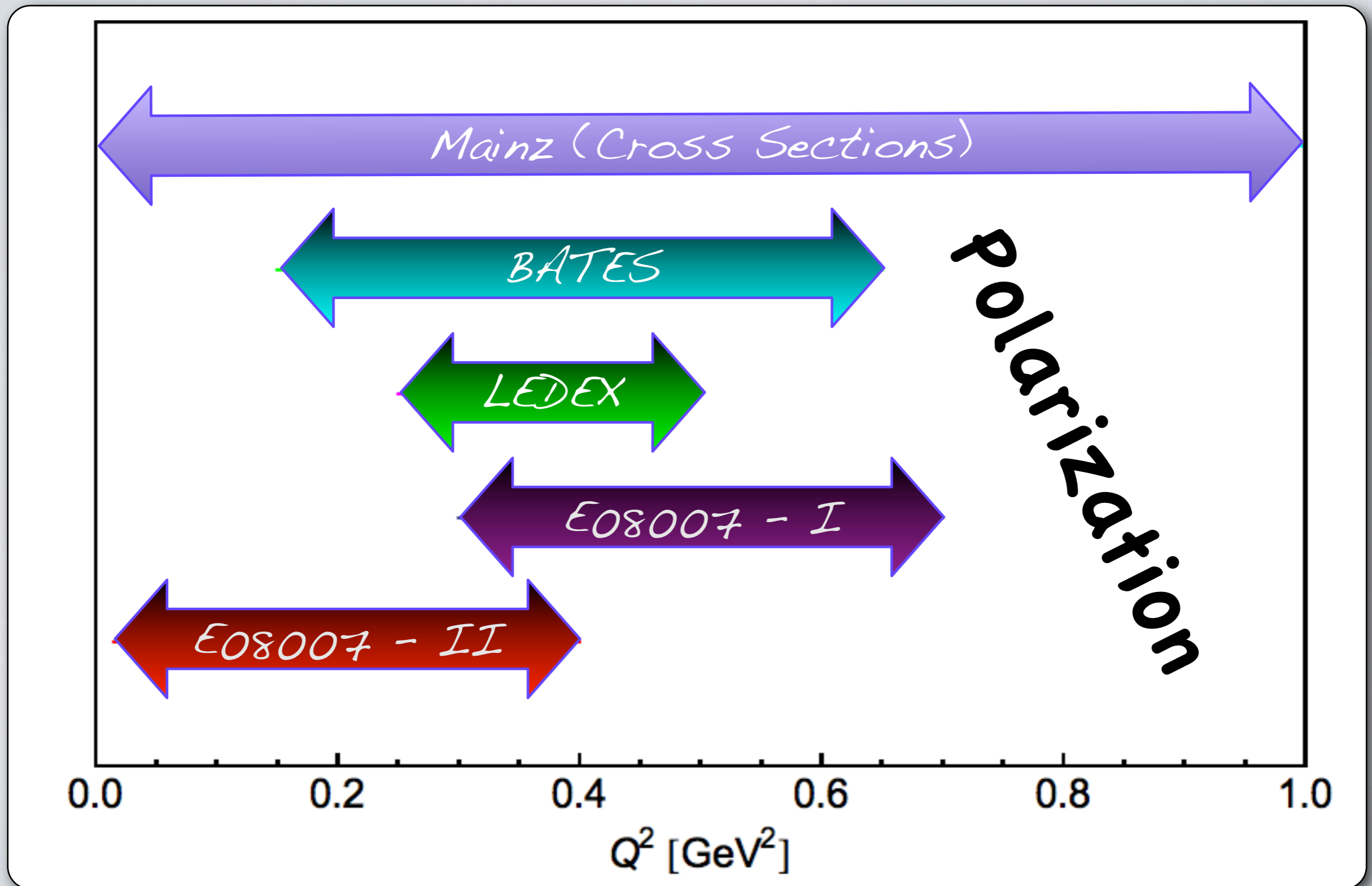
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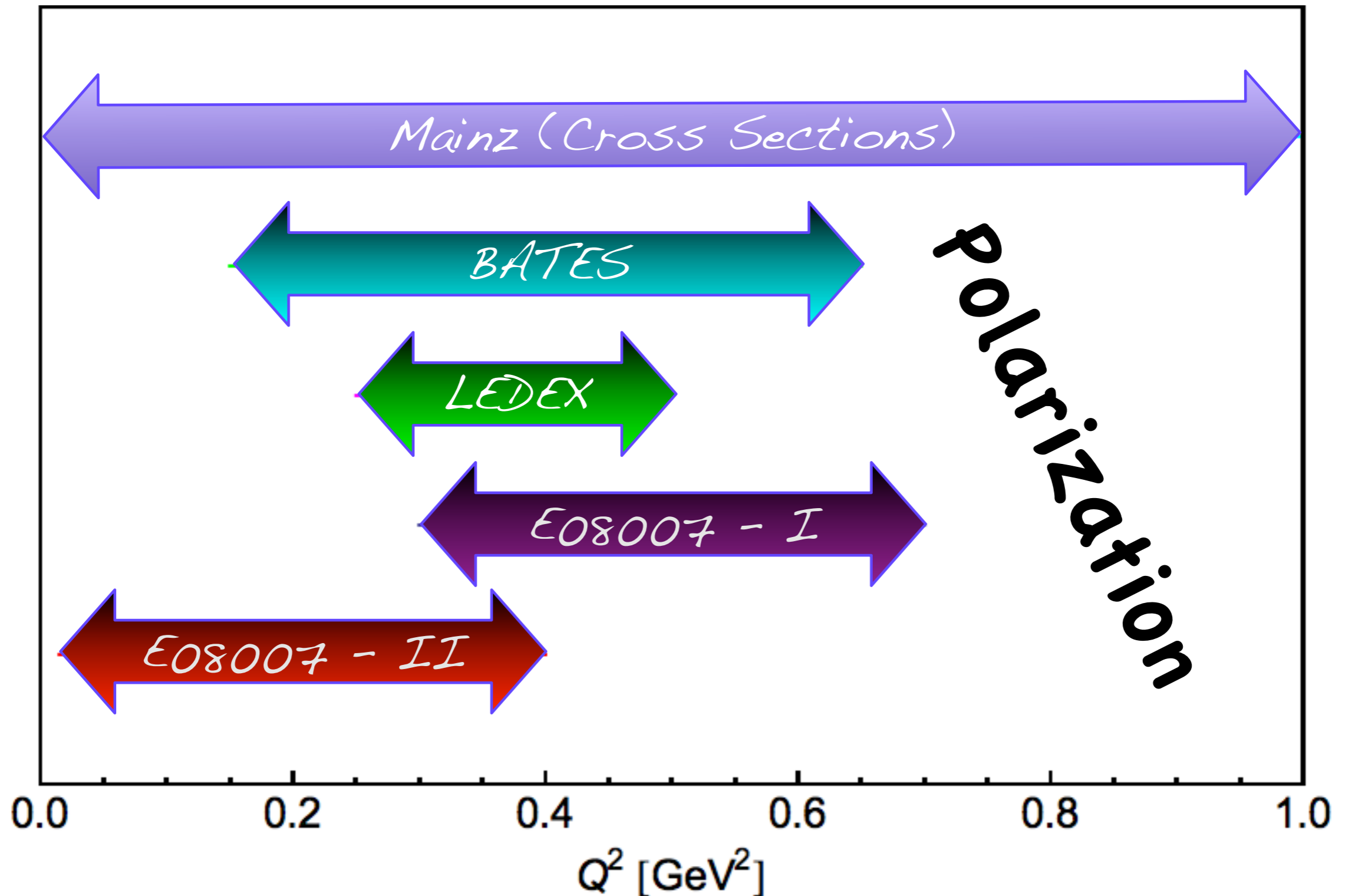


# Comparison to other Experiments Coverage



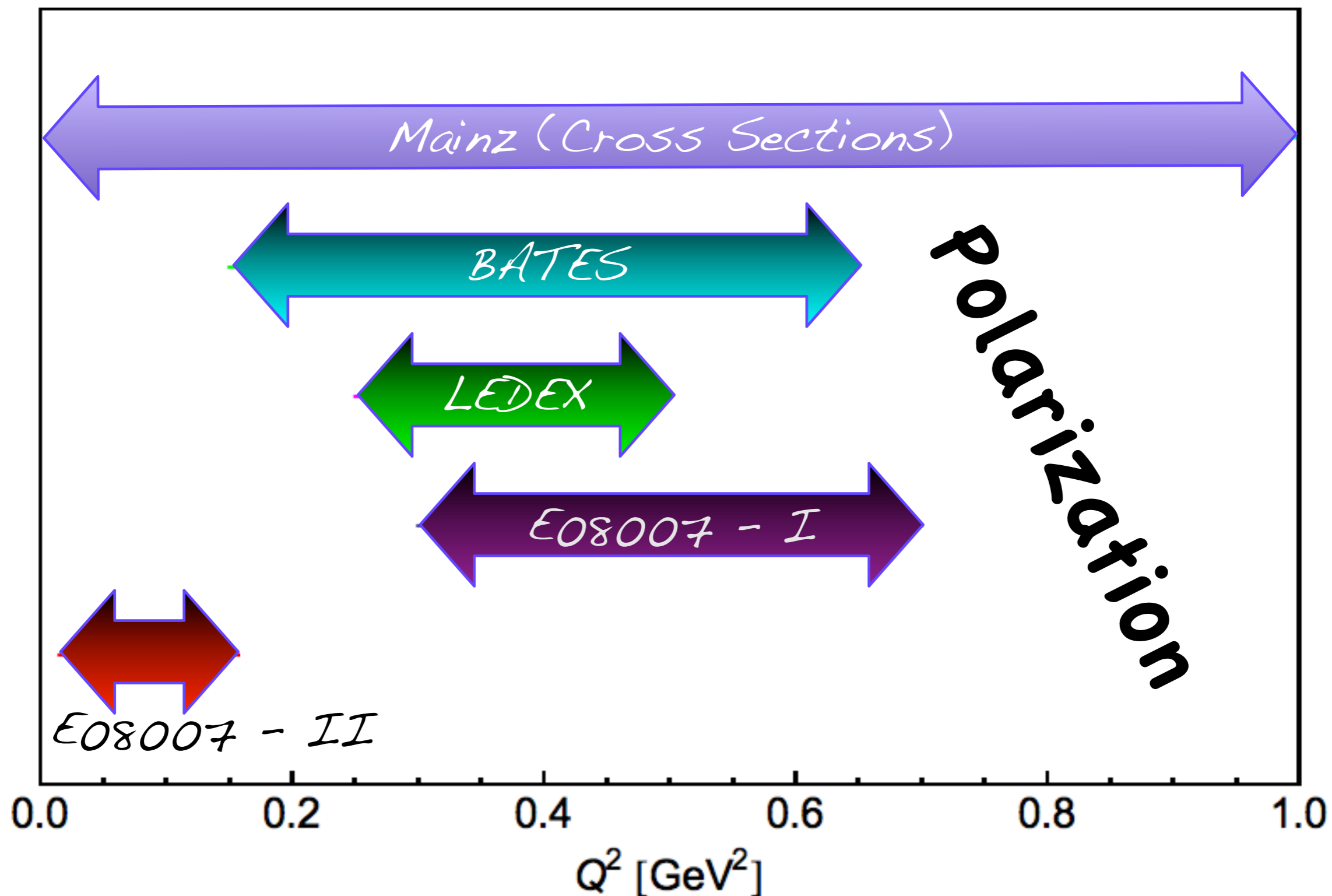
## Complements MAINZ

Overlaps LEDEX, E08007-I - Different technique (systematics)

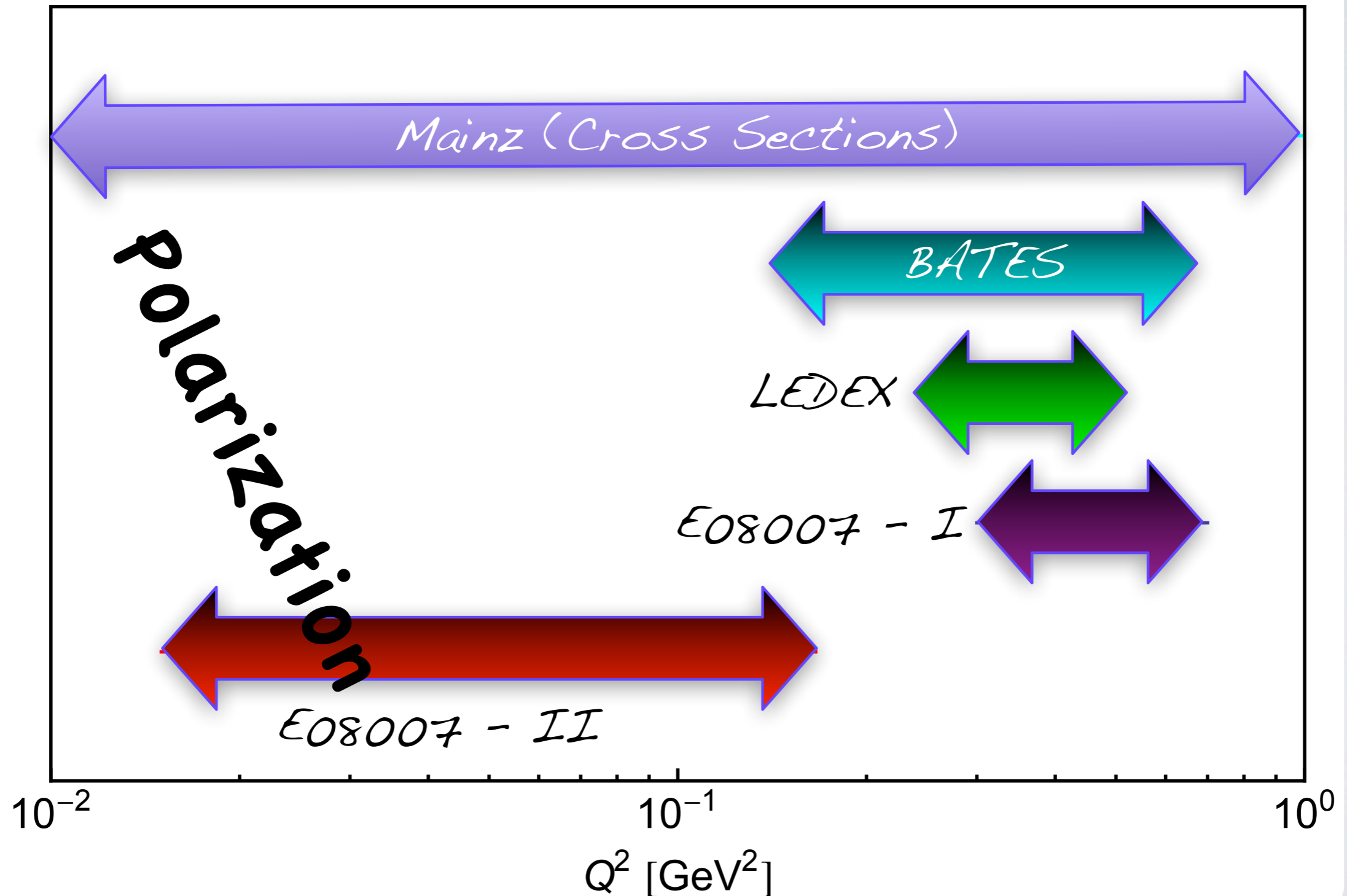


# Complements MAINZ

Does **NOT** Overlap LEDEX, E08007-I

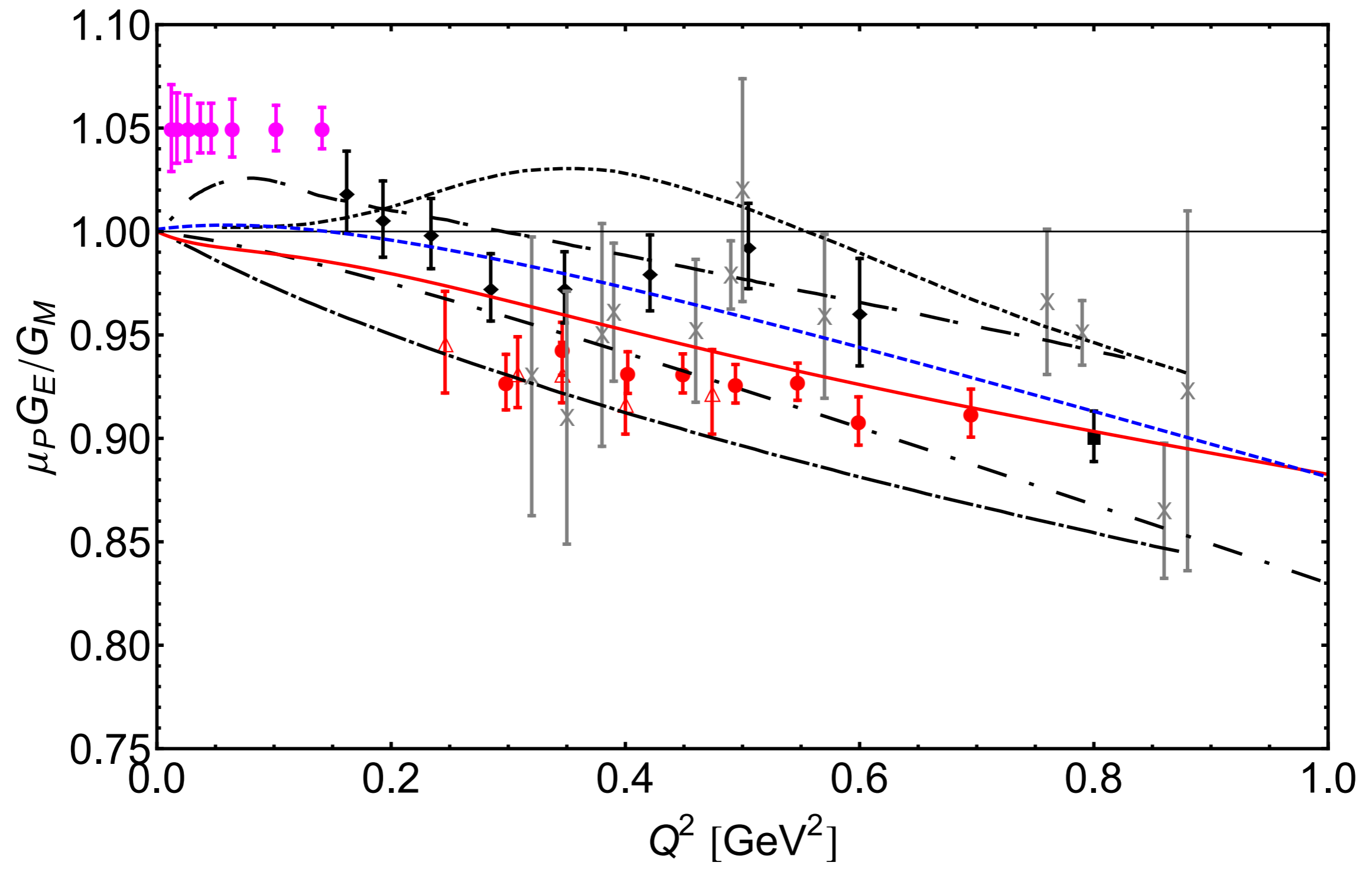


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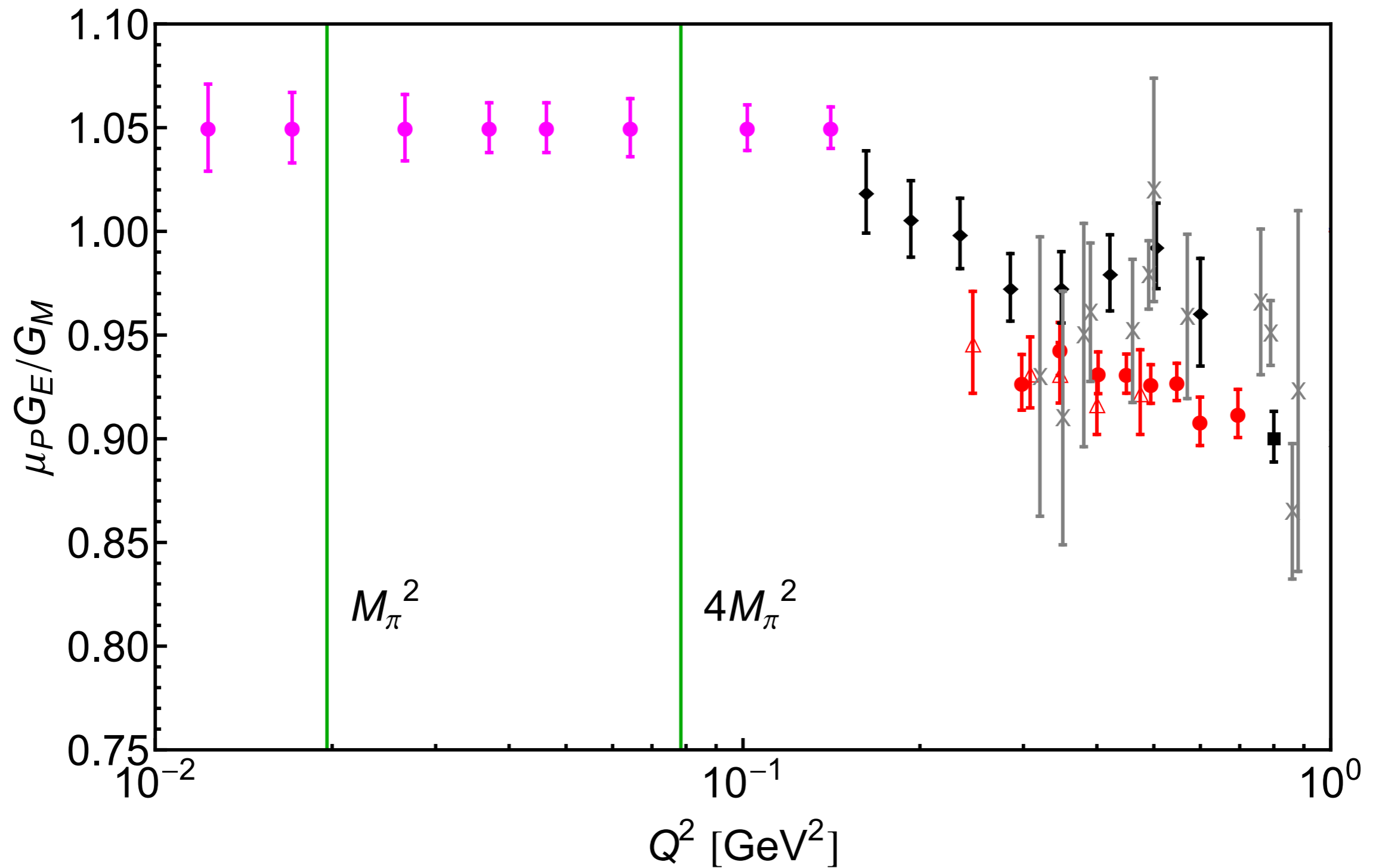
# E08007 - Part II

## Projected uncertainties



# E08007 - Part II

## Projected uncertainties



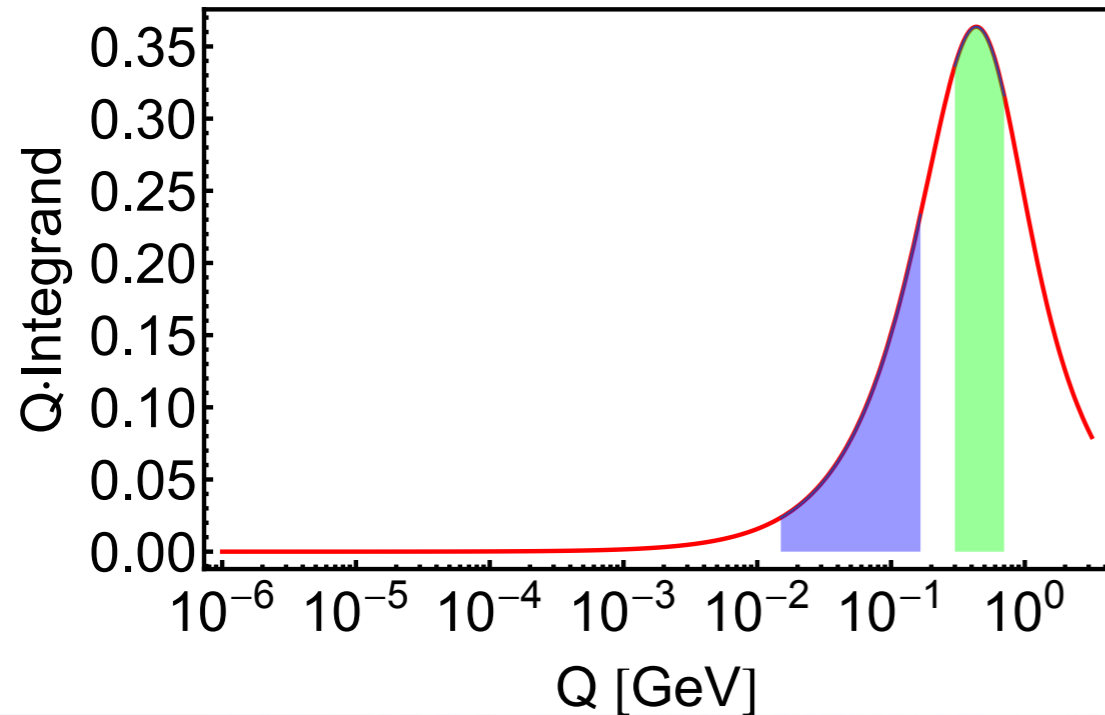
# Zemach Radius

$$E_{hfs} = (1 + \Delta_{QED} + \Delta_{hvp}^p + \Delta_{\mu\nu p}^p + \Delta_{weak}^p + \Delta_S) E_F^p$$

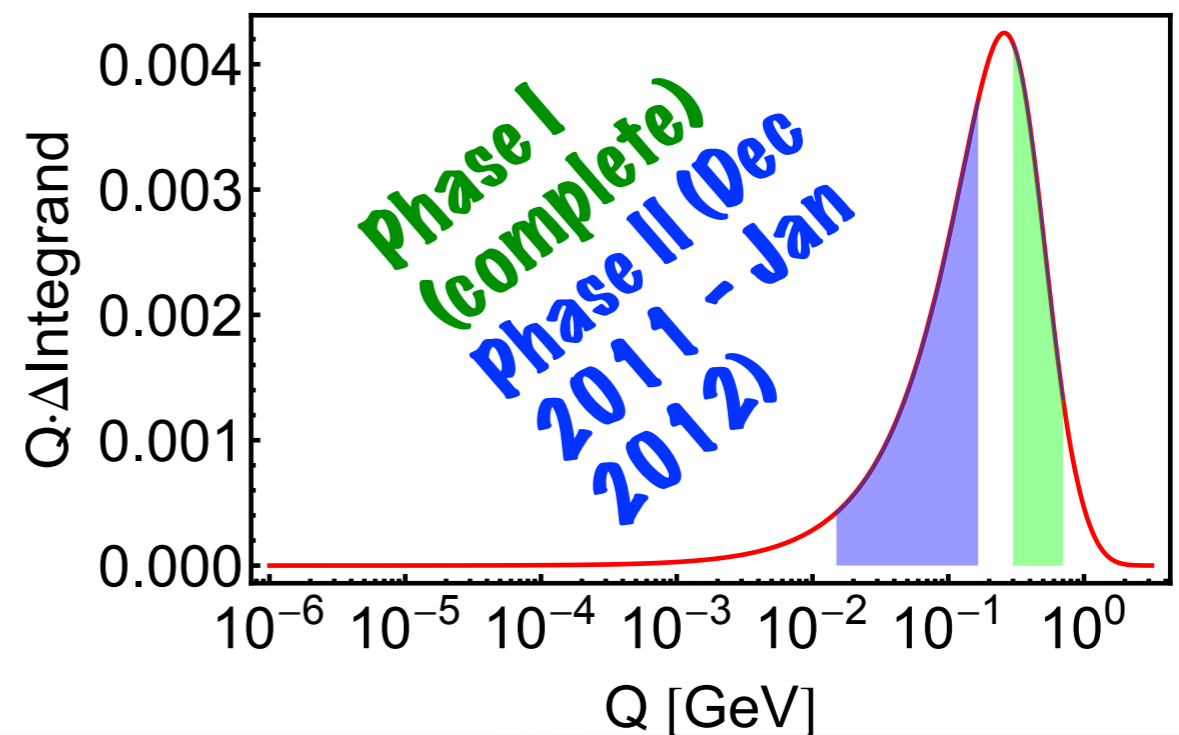
$$\Delta_S = \underline{\Delta_Z} + \Delta_R^p + \Delta_{pol}, \quad \Delta_Z = -2\alpha Z \frac{m_e m_p}{m_e + m_p} r_Z$$

$$r_Z = -\frac{4}{\pi} \int_0^\infty \frac{dQ}{Q^2} [G_E(Q^2) G_M(Q^2) / (1 + \kappa_p) - 1]$$

- $1/Q^2$  term suppresses high  $Q^2$
- $[1 - G_E(Q^2)G_M(Q^2) / \mu_p]$  suppresses lowest  $Q^2$ .
- As  $G_E, G_M$  become small,  $[1 - G_E(Q^2)G_M(Q^2) / \mu_p] \rightarrow 1$ , and the form factor uncertainty has almost no impact on Zemach moment

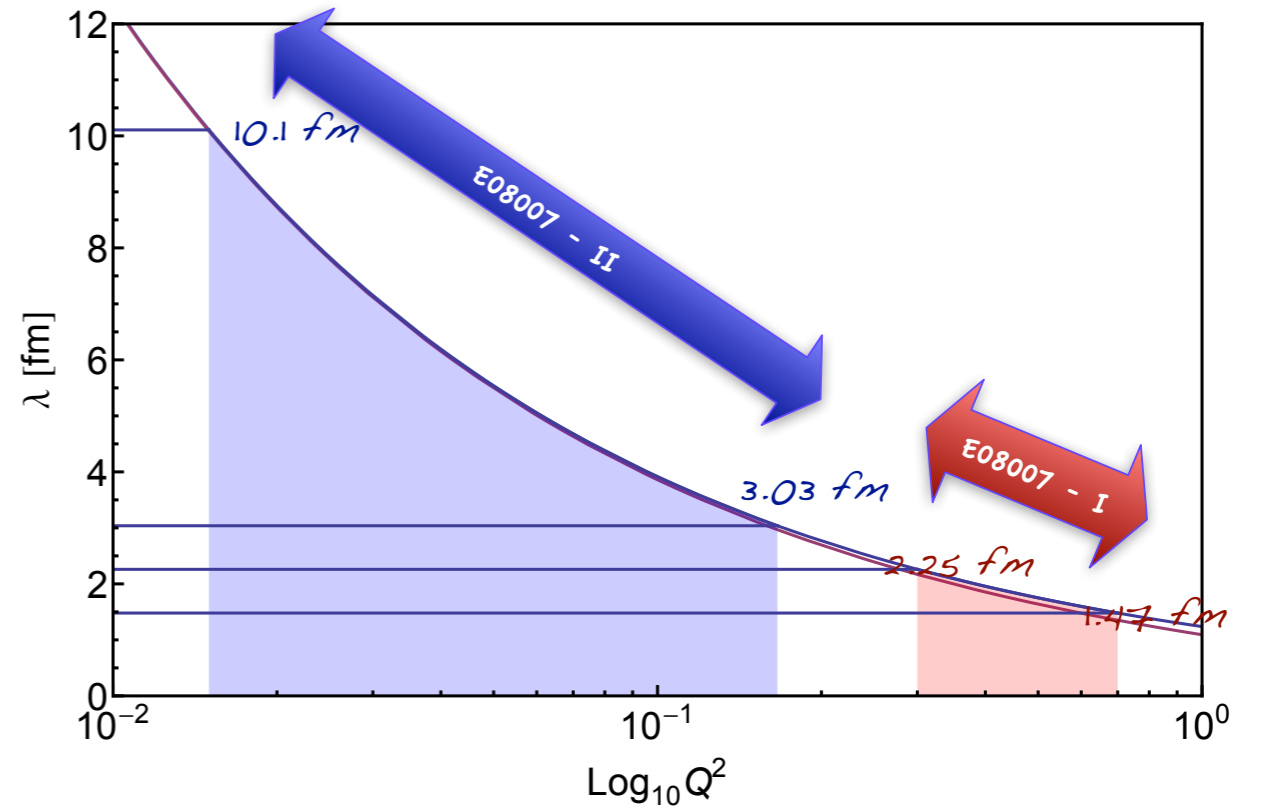
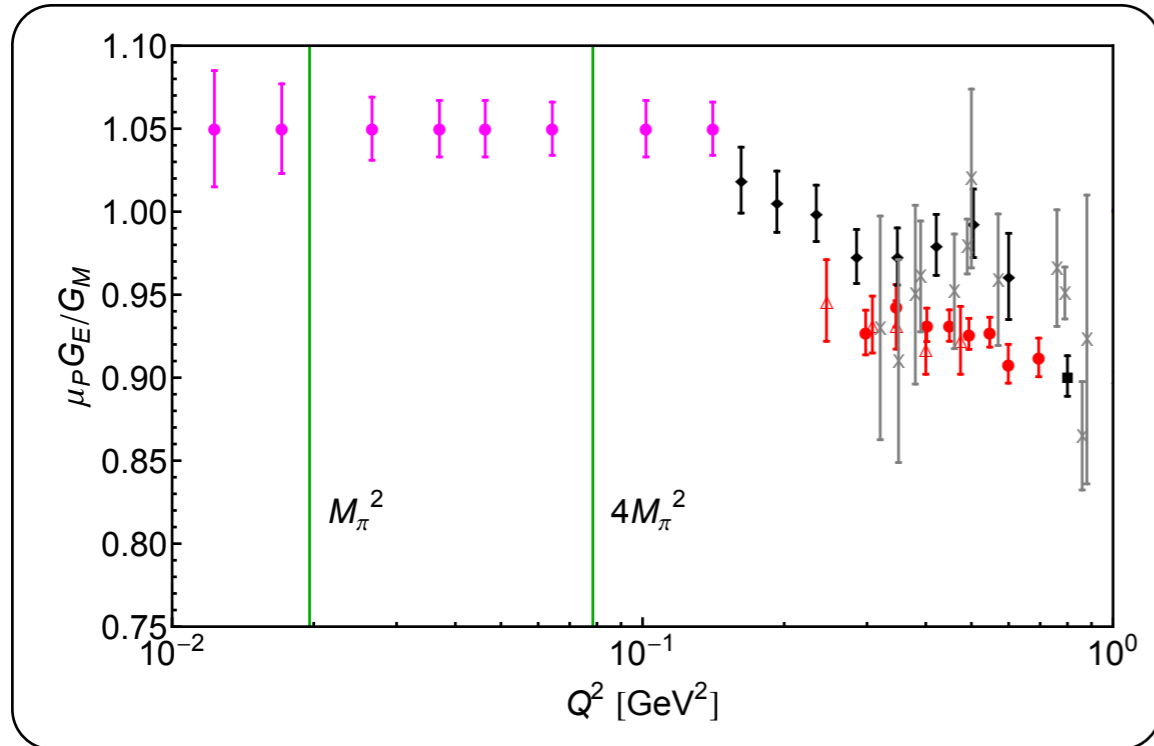
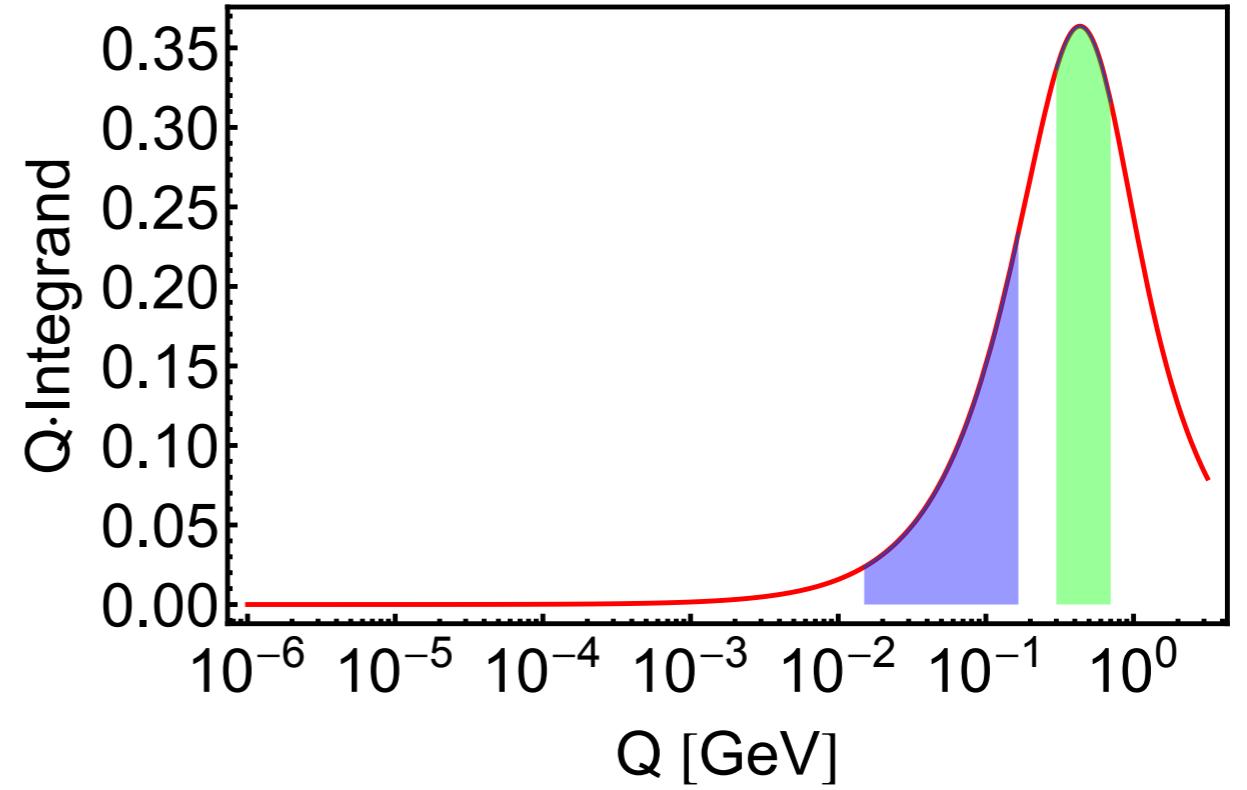
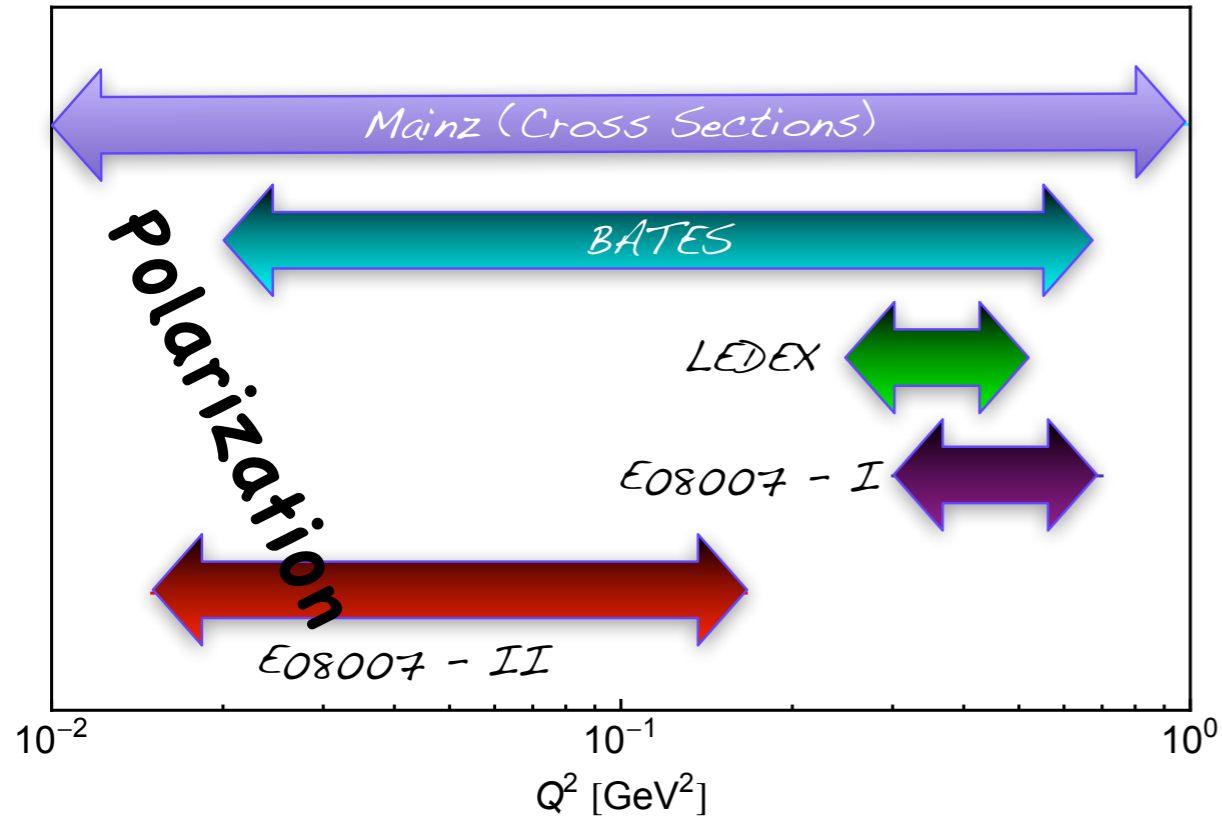


**Significant contribution to integral above  $Q^2=1 \text{ GeV}^2$  and below  $Q^2=0.01 \text{ GeV}^2$**



**Negligible contribution to uncertainty above  $Q^2=1 \text{ GeV}^2$**

# E08007 Coverage





# Summary

- Form factors are physical, model-independent, observable of the nucleon.
- Many discoveries over the years have changed our understanding of one of the basic constituents of matter and still new issues keep popping up.
- While high energy (and  $Q^2$ ) are, of course, important, there is great significance to performing low  $Q^2$  measurements (only real way to discriminate between EFTs).
- Very high precision measurements are now possible and required for high precision experiments.
- It seems that there is no evidence (at least in the FF ratio) for narrow structures.
- One more high precision, low  $Q^2$  experiment before the 12 GeV upgrade. Limited number of candidate facilities for more low  $Q^2$  experiments.

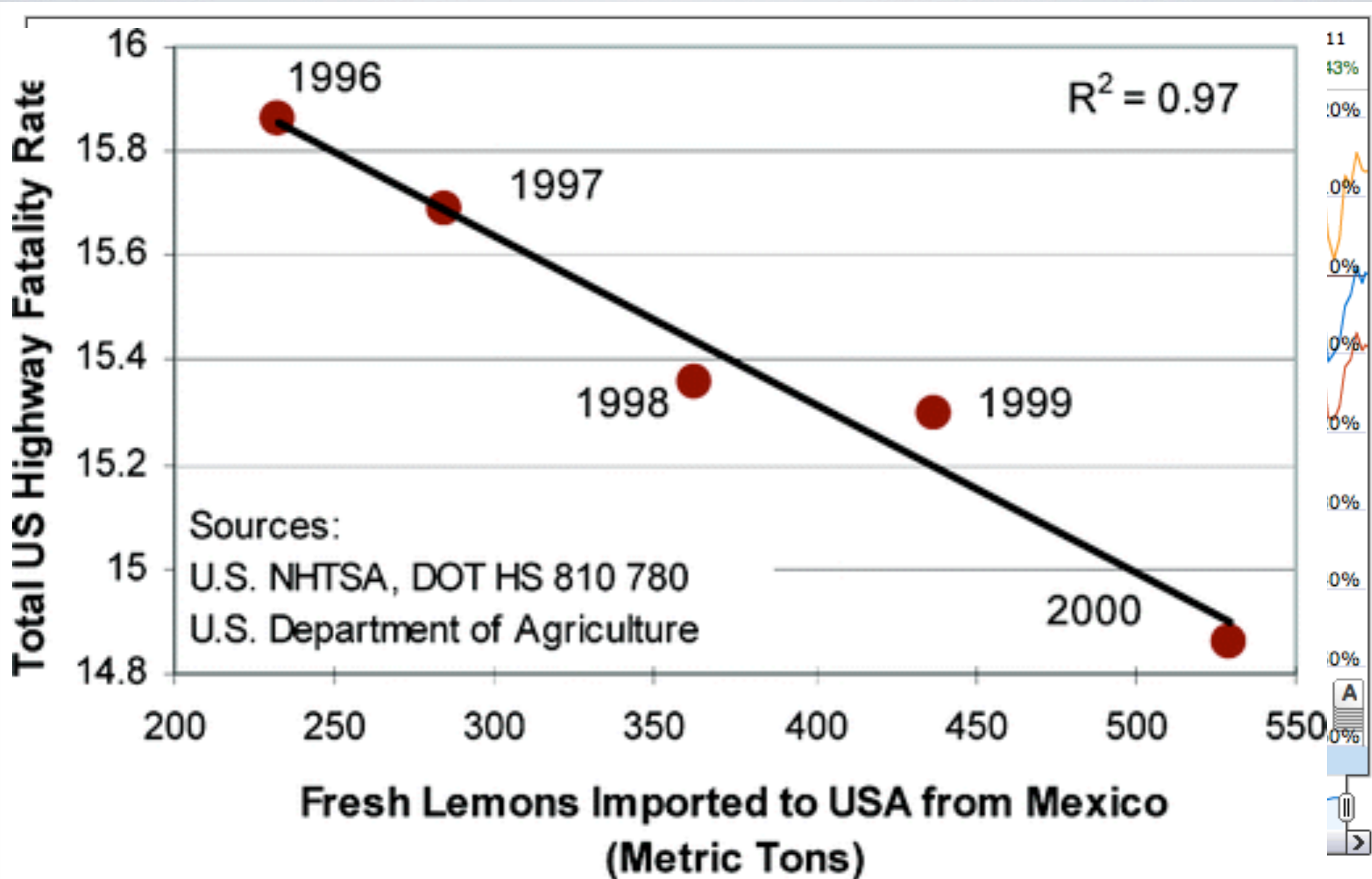
And Finally

# And Finally



[Link to this view](#)

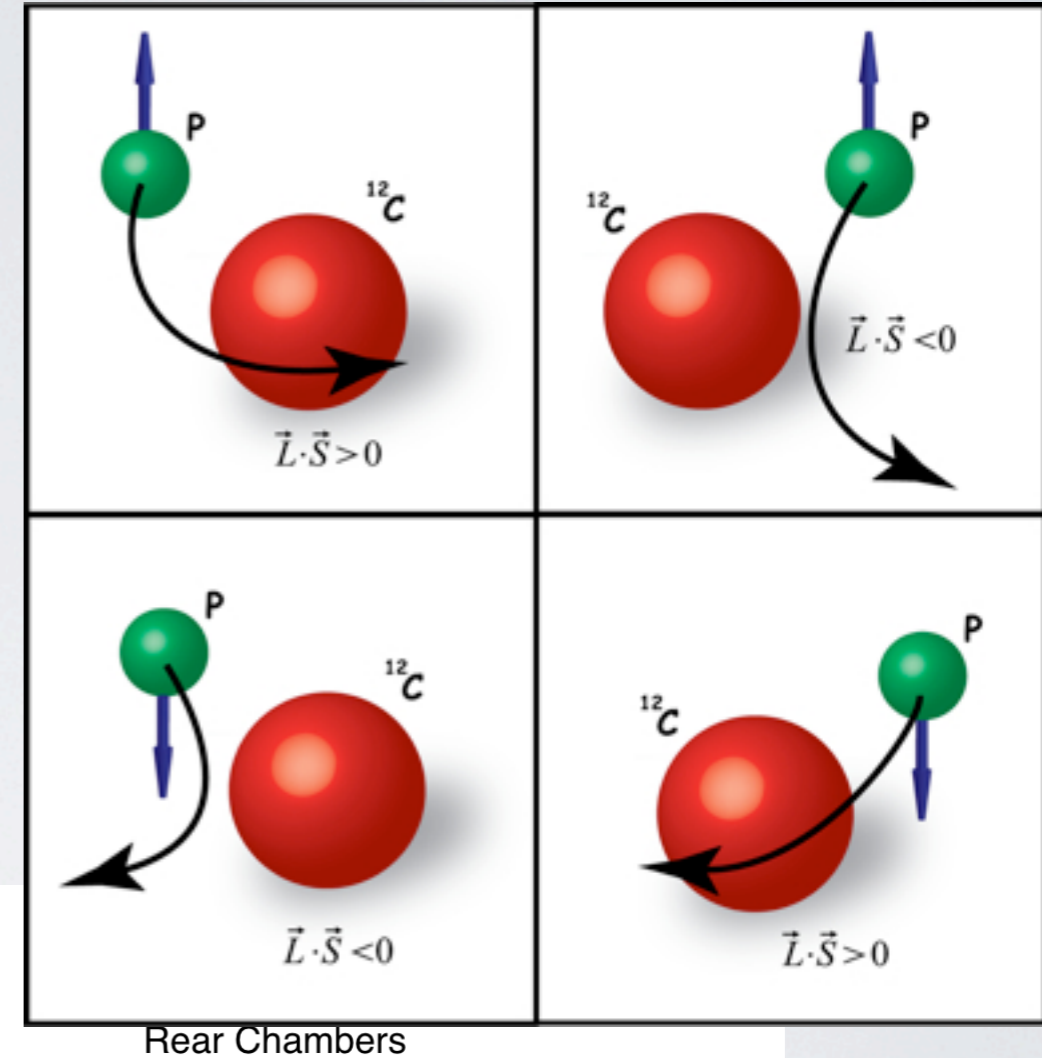
And Finally



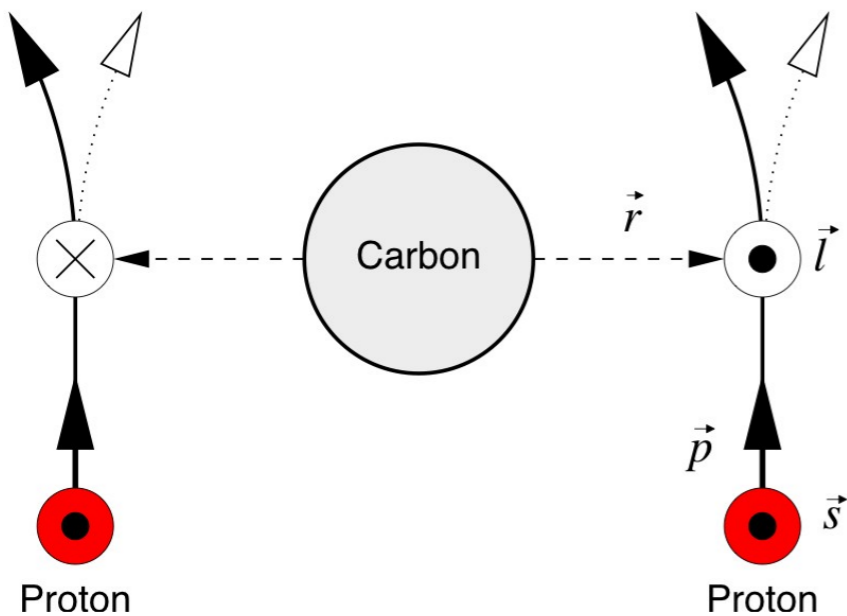
Backup

# How to measure the polarization

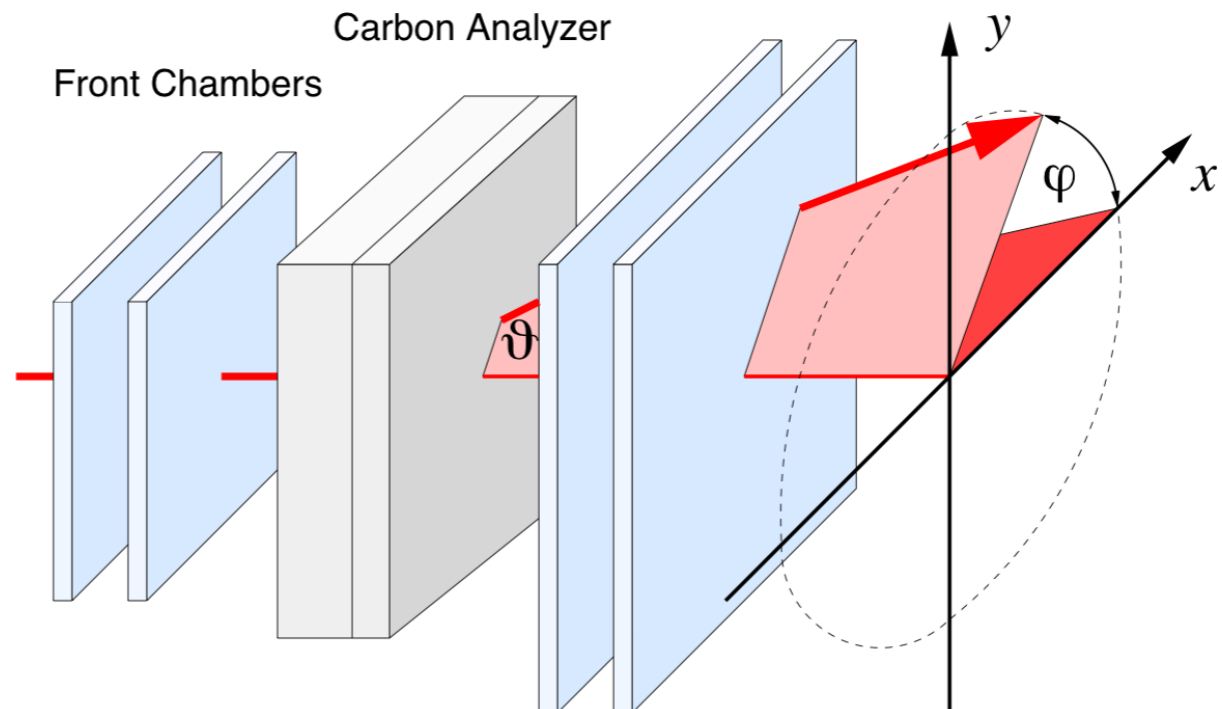
- Scatter recoil nucleons off a nucleus (carbon/hydrogen/...).
- Spin-Orbit coupling causes angular dependence on spin.



Left / right asymmetry

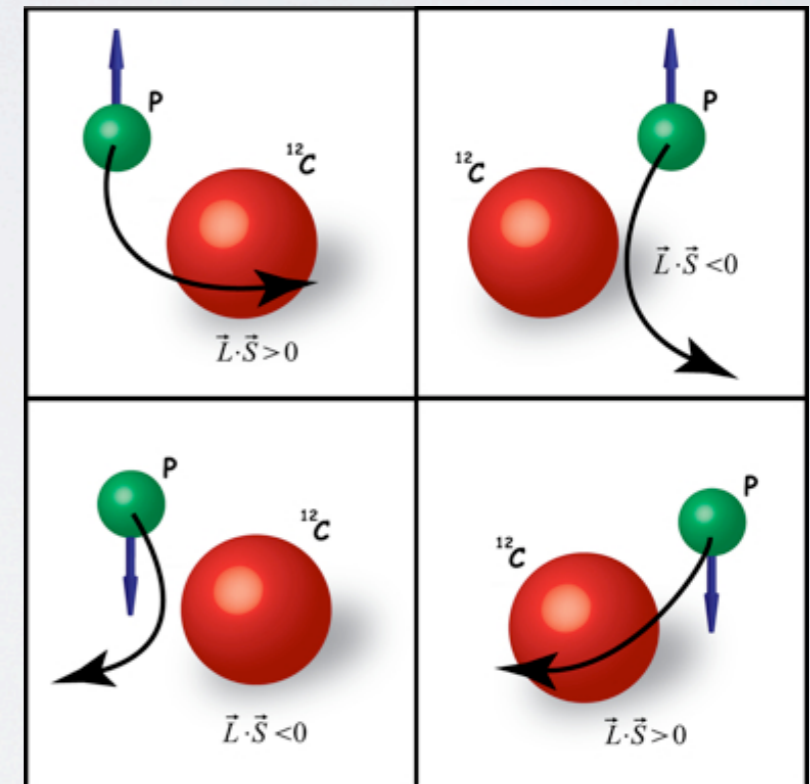


Carbon Analyzer



# How to measure the polarization

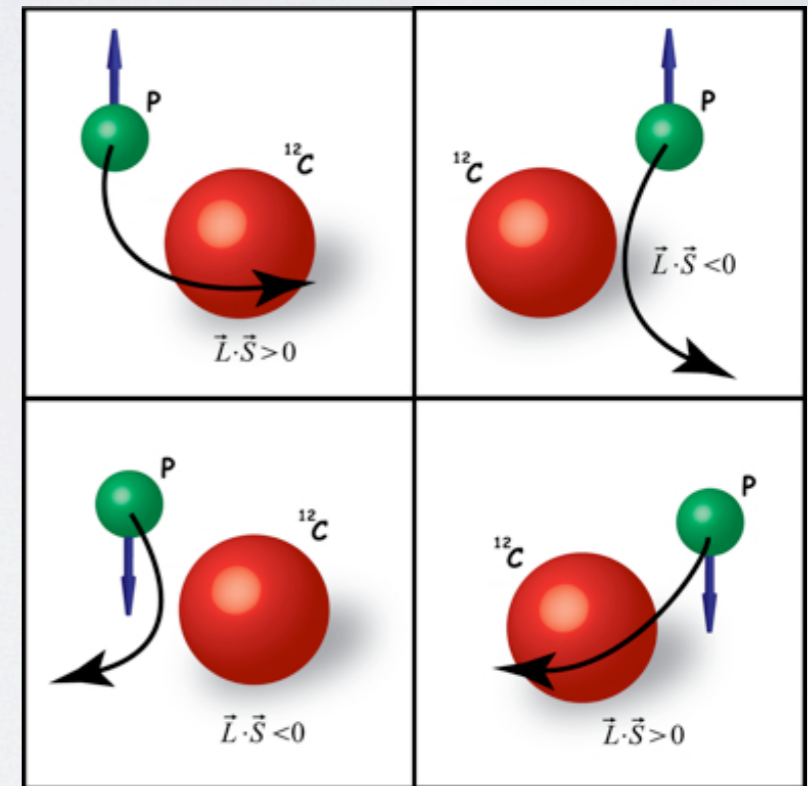
$$N_0(\theta, \phi) = N_0(\theta)\varepsilon(\theta) \left\{ 1 + \left[ hA_y(\theta)P_t^{fpp} + a_{instr} \right] \sin\phi - \left[ hA_y(\theta)P_n^{fpp} + b_{instr} \right] \cos\phi \right\}$$



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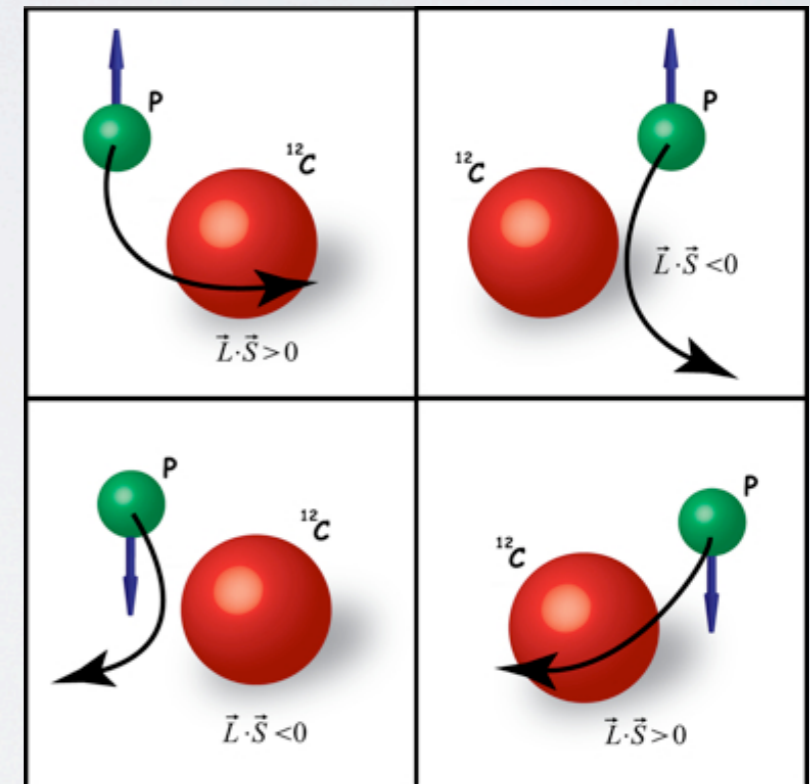


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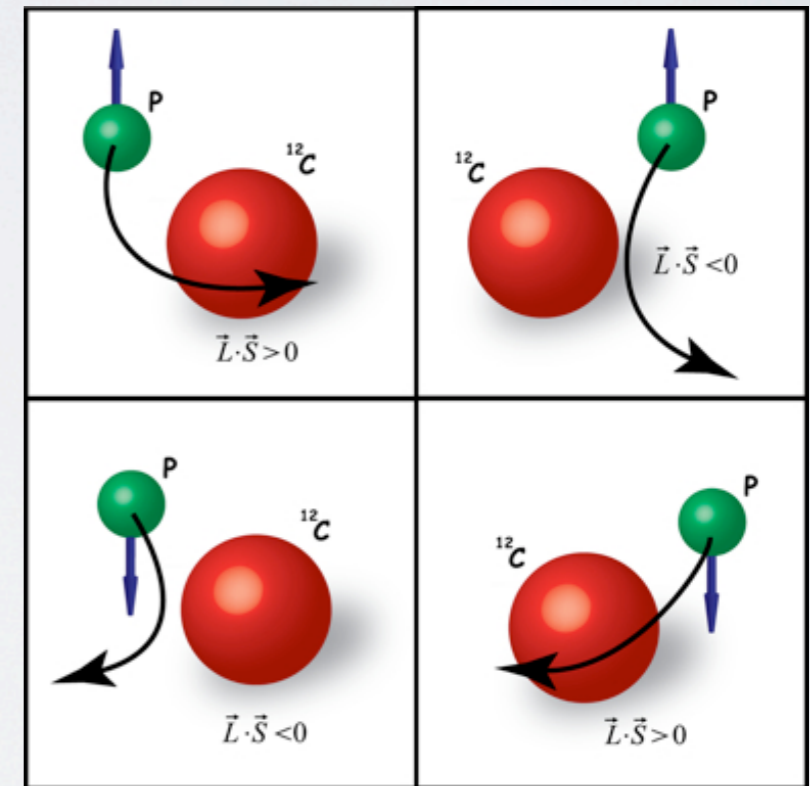


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Systematic uncertainties cancel out  
(to ~0.5%)!

$$\sigma_{stat.} = \sqrt{\frac{2}{N}}$$